



University of Pretoria
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Working Paper: 2019-41

May 2019

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Global Crises and Gold as a Safe Haven: Evidence from Over Seven and a Half Centuries of Data

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Abstract

Using annual data spanning the period of 1258-2018, we test the safe haven characteristic of gold in the wake of global crises. We find that, when we allow for regime-switching to capture nonlinearity and structural breaks, gold serves as a strong hedge against crises, especially during the bullish regime of the market, and in particular from the post-World War I period, as suggested by a time-varying model. In comparison, silver, however, does not seem to possess the safe haven property over the historical period of 1688-2018. Finally, we also find that global crises can accurately predict real gold returns over a long-span (1302-2018) out-of-sample period.

JEL Codes: C22, Q02

Keywords: Global Crises, Gold, Safe Haven, Regime-Switching Model.

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1. Introduction

There exists a large literature that has looked into the “safe haven” status of gold relative to stock, bond and currency markets (see for example, Baur and Lucey (2010), Baur and McDermott (2010), Reboredo (2013a), Agyei-Ampomah et al., (2014), Gürgün and Ünalmis (2014), Beckmann et al., (2015)), as well as oil prices (Reboredo, 2013b; Tiwari et al., 2019). More recently, studies have also analyzed the role of economic uncertainty and geopolitical risks, i.e., non-financial indicators, as drivers of gold prices in the context of its safe haven property (see for example, Baur and Smales (2018), Bouoiyour et al., (2018), Beckmann et al., (2019)).

We aim to build along the latter line of research, by analysing, for the first time, the impact of global crises on (real) gold returns spanning over seven and a half centuries of annual data (1257-2018) using a regime (Markov)-switching model. This approach allows us to test for the safe haven hypothesis of gold in the wake of global crises by controlling for misspecification due to uncaptured nonlinearity, and detects for which regime(s), i.e., bear and/or bull, gold returns increase due to crises over the historical period considered. Unlike the existing studies analysing the safe haven property of gold relying on data post-World War II, we cover the longest possible evolution history of the gold market. In doing so, we avoid any sample selection bias.

The remainder of the paper is organized as follows: Section 2 describes the data, methodology and results, while Section 3 presents additional analyses and Section 4 concludes the paper.

2. Data, Methodology and Results

We use annual data for nominal prices (in British pounds) of gold over 1257 to 2018 retrieved from Measuring Worth.¹ The nominal price of gold was transformed into its real counterpart by deflating with the Consumer Price Index (CPI) derived from a database maintained by the Bank of England called “A Millenium of Macroeconomic Data for the UK”.² We then compute the log-returns of real gold prices, which is plotted in Figure A1 and summarized in Table A1, both of which are included in the Appendix of the paper. As can be seen from Table A1, real gold return (r_{gr}) depicts positive skewness and excess kurtosis, and hence is non-normal, as derived from the strong rejection of the null of normality under the Jarque-Bera test. This provides an initial motivation to look at a regimes-based model. As far as the dates of global crises is concerned, we rely on the information available in Galbraith (1990), Reinhart and Reinhart (2010), and Reihart and Rogoff (2009, 2011), with data beyond 2010 derived from the list of major economic crises available online.³ Table A2 in the Appendix of the paper tabulates the crises. We define a dummy variable, D , which takes the value of one for the dates of crises and zero otherwise.⁴

We start our analysis by estimating a linear regression model of r_{gr} , on D and two lags of r_{gr} as suggested by the Schwarz Information Criterion (SIC).⁵ Using Newey and West (1987) heteroskedasticity and autocorrelation corrected (HAC) standard errors, the coefficient on the dummy was 2.8953 with a p -value of 0.0548. In other words, we found weak (at the 10% level of significance) evidence of gold serving as a safe haven in the wake of global crises. Realizing the

¹ The data is downloadable from: <https://www.measuringworth.com/datasets/gold/>.

² The complete data set is available for download from: <https://www.bankofengland.co.uk/statistics/research-datasets>.

³ See: https://en.wikipedia.org/wiki/List_of_economic_crises.

⁴ Note that, we intentionally leave out the years of the two World Wars from the list, so that these years do not serve as outliers driving our results, and in the process, we concentrate on pure economic and financial crises associated with the extreme behaviour of the general macroeconomic variables and financial markets. However, our results are qualitatively similar if the dummy variable takes a value of one instead of zero for the years associate with the two wars. Complete details of these results are available upon request from the authors.

⁵ We experimented with lagged values of D , but the model fit deteriorated, with lags of D being insignificant. Complete details of these results are available upon request from the authors.

long sample involved in our analysis, we use the Bai and Perron (2003) tests of multiple structural breaks, and detected as many as 5 breaks at 1302, 1340, 1377, 1817 and 1981. We then applied the Brock et al., (1996, BDS) test of nonlinearity on the residuals recovered from the linear regression. As seen from Table A3 in the Appendix, the null of *i.i.d.* is overwhelmingly rejected at the highest level of significance across all dimensions of the test considered, and hence, indicates uncaptured nonlinearity. Given the existence of regimes changes and nonlinearity, it is understandable that the linear model is misspecified, and hence the results derived from it cannot be relied upon. So we next turn our attention to the following Markov-switching model:

$$rgr_t = \alpha_{0,S_t} + \alpha_{1,S_t}rgr_{t-1} + \alpha_{2,S_t}rgr_{t-2} + \alpha_{3,S_t}D_t + \varepsilon_t \quad (1)$$

where $\varepsilon_t \sim iid(0, \sigma_{\varepsilon_t}^2)$ and S_t is a discrete unobservable regime variable taking the values of 1 and 2. The transition between the regime is governed by the first-order Markov process, which means that S_t depend only on the previous regime S_{t-1} as denoted below:

$$p_{ij} = pr(S_t = i / S_{t-1} = j), i, j \in \{1, 2\}.$$

The value p_{ij} is known as the transition probability of moving to state i at t from state j at $t-1$, and is assumed to be independent of time. The transition probabilities must satisfy the condition that $\sum_i p_{ij} = 1$, for all j .

The result from the Markov-Switching model is presented in Table 1. As can be seen gold serves as a safe haven in both regimes with a positive coefficient corresponding to D_t , but the effect is strongly statistically significant at the 1% level in the bull-regime, i.e., Regime 1. Note the effect of crises on gold returns is only significant at the 10% level in the bear-regime, i.e., Regime 2. The smoothed probabilities of Regime 2, as plotted in Figure 1, tends to suggest that the safe haven result is primarily driven by the occurrence of the bull market towards the beginning and end of the sample period.⁶ In sum, our results tend to suggest that while gold does act as a safe haven when a crisis occurs, it does so more strongly during the bull-phases of the market.⁷ In the process, we also highlight the importance of undertaking a nonlinear approach.

[INSERT TABLE 1 AND FIGURE 1]

3. Additional Analyses

In this section, we conduct four additional analyses. First, realizing that the frequency of crises is limited to only one for the period of 1258-1599, we re-estimated our Markov-Switching model over the period of 1600-2018. As reported in Table A4, our results of Table 1 continue to hold with gold serving as a strong safe haven in the bull-regime. Second, we conducted a forecasting exercise, whereby we estimated the model in equation (1) with and without D , and forecasted one-year-ahead in a recursive fashion over the out-of-sample period of 1302-2018 (with an in-sample of 1258-1301), given that the first breakpoint is at 1302. The root mean squared error (RMSE) for the unrestricted (i.e., the model with crises) and restricted (without D) models, was found to be 8.4923 and 8.5657 respectively. In other words, information on global crises also had significant

⁶ The probability of staying in the bull regime, given that the gold market was in the same regime the year before was found to be highly persistent at 94.89%, with an expected duration of about 19.56 years.

⁷ Our result is robust to the usage of nominal gold returns. As a corollary to our analysis of safe haven, when we estimated time-varying persistence of gold returns using the method outlined in Boubaker (2018), we found that persistence was significantly reduced by the crises, which is likely to be an indication of the higher trading in the gold market during episodes of global stress. Complete details of these results are available upon request from the authors.

value⁸ in terms of forecasting of real gold returns. Third, though we know that on average gold strongly acts as a safe haven during the bullish market (dates of which we have exactly identified based on the smoothed regime probabilities), we next use a time-varying model relating rgr and D , estimated using the Kalman filter in a state-space framework (Durbin and Koopman, 2012), to analyze the evolution of gold as a safe haven over our historical sample period. As can be seen from the time-varying coefficient corresponding to D plotted in Figure A2, the effect is predominantly positive with statistical significance observed from the early 1920s (1923 to be exact at the 5% level, and 1918 at the 10% level). This result tends to suggest that gold has been a safe haven primarily, i.e., in the statistical sense, since the end of World War I. Finally, to make our case stronger in favour of gold's unique safe haven characteristic, we also estimated a regime-switching model for the real returns on silver (rsv) over the period of 1688-2018, with the start date being contingent on data availability of silver prices.⁹ Unlike gold, as seen from Table A5, global crises is found to negatively affect real silver returns, though the effect is statistically insignificant.

4. Conclusion

In this paper, we use the longest possible annual data available on gold prices over the period of 1257 to 2018, and test for its safe haven property by analysing the impact of global crises. Using a linear model, we find gold only acts as a weak safe haven, but since we detect nonlinearity and structural breaks, the linear model is misspecified. Next, when we rely on a regime-switching model, we find that gold serves as a strong hedge against risks associated during episodes of crises, especially when the gold market is in a bullish-phase, and in particular from the post-World War I period, as suggested by a time-varying model. In addition, information content of the global crises variable is also found to predict gold returns accurately over a long-span out-of-sample period. In comparison, based on historical data over the period of 1687 to 2018, silver does not seem to possess the safe haven property. Our paper thus, provides overwhelming support of gold being a safe haven relative to global crises, by tracking the longest possible historical evolution of this market possible.

⁸ McCracken's (2007) *MSE-F* statistic of forecast comparison across nested models produced a corresponding value of 12.2354, which was significant at the 1% level of significance.

⁹ As with gold, nominal silver prices in British pounds were also derived from Measuring Worth, and converted to real values by deflating with the CPI.

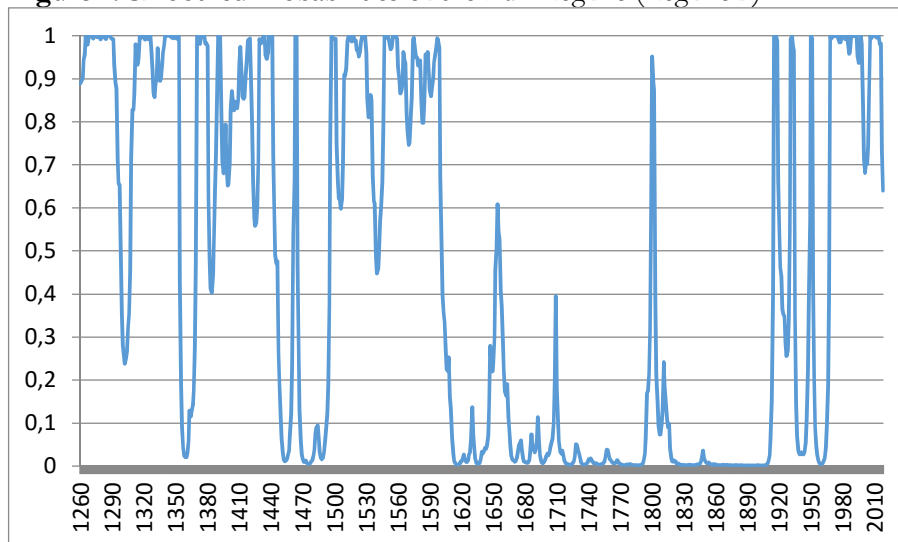
References

- Agyei-Ampomah, S., Gounopoulos, D. and Mazouz, K. (2014). Does gold offer a better protection against sovereign debt crisis than other metals? *Journal of Banking & Finance*, 40, 507-521.
- Bai, J. and Perron, P. 2003. Computation and analysis of multiple structural change models. *Journal of Applied Econometrics*, 18, 1-22.
- Baur, D.G. and Lucey, B.M. (2010) Is gold a hedge or a safe haven? An analysis of stocks, bonds and gold. *The Financial Review*, 45, 217-229.
- Baur, D.G. and McDermott, T.K. (2010). Is gold a safe haven? International evidence. *Journal of Banking & Finance*, 34, 1886-1898.
- Baur, D.G., and Smales, L. (2018). Gold and Geopolitical Risk. Available at SSRN: <https://ssrn.com/abstract=3109136>.
- Beckmann, J., Berger, T. and Czudaj, R. (2015) Does gold act a hedge or safe haven for stocks? A smooth transition approach. *Economic Modelling* 48, 16-24
- Beckmann, J., Berger, T., and Czudaj, R. (2019). Gold Price Dynamics and the Role of Uncertainty. *Quantitative Finance*, 19(4), 663-681.
- Boubaker, H. (2018). A Generalized ARFIMA Model with Smooth Transition Fractional Integration Parameter. *Journal of Time Series Econometrics*, 10(1), 1-20.
- Bouoiyour, J., Selmi, R., and Wohar, M.E. (2018). Measuring the response of gold prices to uncertainty: An analysis beyond the mean. *Economic Modelling*, 75(C), 105-116.
- Brock, W., Dechert, D., Scheinkman, J., and LeBaron, B. (1996). A test for independence based on the correlation dimension. *Econometric Reviews*, 15, 197–235.
- Durbin, J., and Koopman, S.J. (2012). *Time Series Analysis by State Space Methods*. Second Edition, Oxford: Oxford University Press.
- Galbraith, J.K. (1990). *A Short History of Financial Euphoria*. New York: Penguin Books.
- Gürgün, G. and Ünalmsı, I. (2014) Is gold a safe haven against equity market investment in emerging and developing countries? *Finance Research Letters*, 11, 341-348.
- McCracken, M.W. (2007). Asymptotics for out of sample tests of Granger causality. *Journal of Econometrics*, 140, 719-752
- Newey, W.K., and West, K.D. (1987). A Simple, Positive Semi-definite, Heteroskedasticity and Autocorrelation Consistent Covariance Matrix. *Econometrica*, 55(3), 703–708.
- Reboredo, J.C. (2013a). Is gold a safe haven or a hedge for the US dollar? Implications for risk management. *Journal of Banking & Finance*, 37(8), 2665-2676.
- Reboredo, J.C. (2013b). Is gold a hedge or safe haven against oil price movements? *Resources Policy* 38(2), 130-137.
- Reinhart, C.M., and Reinhart, V.R. (2010). After the fall. *Proceedings, Economic Policy Symposium, Jackson Hole, Federal Reserve Bank of Kansas City*, 17-60.
- Reinhart, C.M., and Rogoff, K.S. (2009). *This Time is Different: Eight Centuries of Financial Folly*. Princeton University Press, Princeton, USA.
- Reinhart, C.M., and Rogoff, K.S. (2011). From Financial Crash to Debt Crisis. *American Economic Review*, 101(5), 1676-1706.
- Tiwari, A.K., Aye, G.C., Gupta, R., and Gkillas, K. (2019). Gold-Oil Dependence Dynamics and the Role of Geopolitical Risks: Evidence from a Markov-Switching Time-Varying Copula Model. Department of Economics, University of Pretoria, Working Paper No. 201918.

Table 1. Markov-Switching Model Estimates for Real Gold Returns (1258-2018)

| Coefficient | Estimate | Std. Error | z-Statistic | Prob. |
|------------------------------|----------|----------------|-------------|-----------|
| Regime 1 | | | | |
| α_{01} | -0.4216 | 0.2563 | -1.6448 | 0.1000 |
| α_{31} | 1.0872 | 0.6468 | 1.6809 | 0.0928 |
| α_{11} | 0.1833 | 0.0542 | 3.3837 | 0.0007 |
| α_{21} | -0.2297 | 0.0474 | -4.8469 | 0.0000 |
| $\log(\sigma_1)$ | 1.4786 | 0.0514 | 28.7745 | 0.0000 |
| Regime 2 | | | | |
| α_{02} | -0.3058 | 0.7182 | -0.4258 | 0.6702 |
| α_{32} | 5.4254 | 2.0315 | 2.6706 | 0.0076 |
| α_{12} | 0.1223 | 0.0555 | 2.2030 | 0.0276 |
| α_{22} | -0.2107 | 0.0573 | -3.6770 | 0.0002 |
| $\log(\sigma_2)$ | 2.4800 | 0.0542 | 45.7280 | 0.0000 |
| Transition Matrix Parameters | | | | |
| $p_{0,11}$ | 3.1316 | 0.4246 | 7.3762 | 0.0000 |
| $p_{0,21}$ | -2.9210 | 0.5448 | -5.3617 | 0.0000 |
| Mean rgr | 0.020206 | S.D. rgr | | 8.929976 |
| S.E. of regression | 8.652950 | SSR | | 56080.28 |
| Durbin-Watson stat | 2.027459 | Log likelihood | | -2597.270 |
| AIC | 6.875546 | SIC | | 6.948779 |

Note: Estimates correspond to: $rgr_t = \alpha_{0,s_t} + \alpha_{1,s_t}rgr_{t-1} + \alpha_{2,s_t}rgr_{t-2} + \alpha_{3,s_t}D_t + \varepsilon_t$, where rgr is real gold log-returns.

Figure 1. Smoothed Probabilities of the Bull-Regime (Regime 2):

APPENDIX:

Table A1. Summary Statistics

| Statistic | <i>rgr</i> |
|-----------------|------------|
| Mean | 0.0267 |
| Median | -0.3983 |
| Maximum | 44.7947 |
| Minimum | -28.4885 |
| Std. Dev. | 8.9191 |
| Skewness | 0.6113 |
| Kurtosis | 6.0658 |
| Jarque-Bera | 345.4142 |
| <i>p</i> -value | 0.0000 |
| Observations | 761 |

Note: *rgr*: real gold log-returns; Std. Dev.: Standard deviation; *p*-value: probability of the Jarque-Bera test with the null of normality.

Table A2. List of Global Crises

| Crises | Date |
|--|-----------|
| 14th century banking crisis | 1345 |
| The century Kipper und Wipper financial crisis | 1618–1622 |
| Tulip mania bubble | 1637 |
| The General Crisis | 1640 |
| Great Tobacco Depression | 1703 |
| South Sea Bubble | 1720 |
| Mississippi Company | 1720 |
| Crisis of 1763 | 1763 |
| Great East Indian Bengal Bubble Crash | 1769 |
| Crisis of 1772 | 1772 |
| War of American Independence Financing Crisis | 1776 |
| Panic of 1785 | 1785 |
| Panic of 1792 | 1792 |
| Panic of 1796–1797 | 1796–1797 |
| Danish state bankruptcy | 1813 |
| Post-Napoleonic depression | 1815 |
| Panic of 1819 | 1819 |
| Panic of 1825 | 1825 |
| Panic of 1837 | 1837 |
| Panic of 1847 | 1847 |
| Panic of 1857 | 1857 |
| Panic of 1866 | 1866 |
| Great Depression of British Agriculture | 1873–1896 |
| Long Depression | 1873–1896 |

| | |
|--|------------------------|
| Panic of 1901 | 1901 |
| Panic of 1907 | 1907 |
| Depression of 1920-21 | 1920-1921 |
| Wall Street Crash of 1929 and Great Depression | 1929–1939 |
| OPEC oil price shock | 1973 |
| Energy crisis | 1979 |
| Secondary banking crisis | 1973–1975 |
| Early 1980s Recession | 1981-1982 |
| Latin American debt crisis | 1982 |
| Bank stock crisis | 1983 |
| Japanese asset price bubble | 1986–1992 |
| Black Monday | 1987 |
| Savings and loan crisis | 1986–1995 |
| Special Period in Cuba | 1990–1994 |
| India economic crisis | 1991 |
| Finnish banking crisis | 1991-1993 |
| Swedish banking crisis | 1990 |
| Economic crisis in Mexico | 1994 |
| Asian financial crisis | 1997 |
| Russian financial crisis | 1998 |
| Ecuador financial crisis | 1998-1999 |
| Argentine economic crisis | 1999–2002 |
| Samba effect | 1999 |
| Dot-com bubble | 2000-2002 |
| Turkish economic crisis | 2001 |
| Uruguay banking crisis | 2002 |
| Venezuelan general strike | 2002–2003 |
| Financial Crisis | 2007-2009 |
| 2000s energy crisis | 2003-2009 |
| Subprime mortgage crisis | 2007-2010 |
| United States housing bubble and United States housing market correction | 2003-2011 |
| Automotive industry crisis | 2008–2010 |
| Icelandic financial crisis | 2008–2012 |
| Irish banking crisis | 2008–2010 |
| Russian financial crisis | 2008–2009 |
| Latvian financial crisis | 2008 |
| Venezuelan banking crisis | 2009–2010 |
| Spanish financial crisis | 2008-2016 |
| European sovereign debt crisis | 2009-2018, and ongoing |
| Portuguese financial crisis | 2010-2014 |
| Crisis in Venezuela | 2012-2018, and ongoing |

| | |
|----------------------------------|------------------------|
| Ukrainian crisis | 2013-2014 |
| Russian financial crisis | 2014 |
| Brazilian economic crisis | 2014-2017 |
| Chinese stock market crash | 2015 |
| Turkish currency and debt crisis | 2018 |
| Debt crisis in India | 1993-2018, and ongoing |

Sources: Galbraith (1990), Reinhart and Reinhart (2010), and Reinhart and Rogoff (2009, 2011), with data beyond 2010 derived from the list of major economic crises available online at: https://en.wikipedia.org/wiki/List_of_economic_crises.

Table A3. Brock et al., (1996, BDS) Test of Nonlinearity

| Independent Variable | Dimension | | | | |
|----------------------|-------------|-------------|-------------|-------------|-------------|
| | 2 | 3 | 4 | 5 | 6 |
| <i>rgr</i> | 8.089194*** | 10.15849*** | 11.32392*** | 12.67988*** | 13.74119*** |

Note: Entries correspond to the $\hat{\zeta}$ -statistic of the BDS test with the null of *i.i.d.* residuals, with the test applied to the residuals recovered from the real gold returns (*rgr*) equation with two lags of gold returns and the contemporaneous crises dummy; * indicates rejection of the null hypothesis at 1 percent level of significance.

Table A4. Markov-Switching Model Estimates for Real Gold Returns (1600-2018)

| Coefficient | Estimate | Std. Error | χ^2 -Statistic | Prob. |
|------------------------------|----------|----------------|---------------------|--------|
| Regime 1 | | | | |
| α_{01} | -0.4872 | 0.2686 | -1.8134 | 0.0698 |
| α_{31} | 1.2527 | 0.6310 | 1.9852 | 0.0471 |
| α_{11} | 0.2305 | 0.0527 | 4.3758 | 0.0000 |
| α_{21} | -0.1969 | 0.0502 | -3.9267 | 0.0001 |
| $\log(\sigma_1)$ | 1.4680 | 0.0456 | 32.1727 | 0.0000 |
| Regime 2 | | | | |
| α_{02} | -1.3736 | 3.0619 | -0.4486 | 0.6537 |
| α_{32} | 5.4103 | 4.2160 | 1.2833 | 0.1994 |
| α_{12} | 0.4356 | 0.1262 | 3.4508 | 0.0006 |
| α_{22} | -0.2981 | 0.1339 | -2.2257 | 0.0260 |
| $\log(\sigma_2)$ | 2.7522 | 0.0994 | 27.6852 | 0.0000 |
| Transition Matrix Parameters | | | | |
| $p_{0,11}$ | 3.7404 | 0.4925 | 7.5944 | 0.0000 |
| $p_{0,21}$ | -1.9560 | 0.5215 | -3.7506 | 0.0002 |
| Mean rgr | 0.081765 | S.D. rgr | 8.178857 | |
| S.E. of regression | 7.527664 | SSR | 23176.28 | |
| Durbin-Watson stat | 1.948417 | Log likelihood | -1330.120 | |
| AIC | 6.406302 | SIC | 6.521945 | |

Note: Estimates correspond to: $rgr_t = \alpha_{0,S_t} + \alpha_{1,S_t}rgr_{t-1} + \alpha_{2,S_t}rgr_{t-2} + \alpha_{3,S_t}D_t + \varepsilon_t$, where rgr is real gold log-returns.

Table A5. Markov-Switching Model Estimates for Real Silver Returns (1688-2018)

| Coefficient | Estimate | Std. Error | z -Statistic | Prob. |
|------------------------------|-----------|----------------|----------------|-----------|
| Regime 1 | | | | |
| α_{01} | -0.5752 | 0.3802 | -1.5130 | 0.1303 |
| α_{31} | -0.2166 | 1.0228 | -0.2118 | 0.8323 |
| α_{11} | 0.2048 | 0.0608 | 3.3661 | 0.0008 |
| α_{21} | -0.3101 | 0.0595 | -5.2143 | 0.0000 |
| $\log(\sigma_1)$ | 1.6159 | 0.0699 | 23.1174 | 0.0000 |
| Regime 2 | | | | |
| α_{02} | 0.2781 | 3.2128 | 0.0866 | 0.9310 |
| α_{32} | -0.6952 | 4.3598 | -0.1595 | 0.8733 |
| α_{12} | 0.1352 | 0.1027 | 1.3162 | 0.1881 |
| α_{22} | -0.2357 | 0.1028 | -2.2918 | 0.0219 |
| $\log(\sigma_2)$ | 3.0339 | 0.0819 | 37.0398 | 0.0000 |
| Transition Matrix Parameters | | | | |
| $p_{0,11}$ | 4.6655 | 0.8564 | 5.4478 | 0.0000 |
| $p_{0,21}$ | -3.9169 | 0.9149 | -4.2811 | 0.0000 |
| Mean rsr | -0.426462 | S.D. rsr | | 12.53536 |
| S.E. of regression | 12.21342 | SSR | | 47584.46 |
| Durbin-Watson stat | 2.019815 | Log likelihood | | -1149.971 |
| AIC | 7.063653 | SIC | | 7.202111 |

Note: Estimates correspond to: $rsr_t = \alpha_{0,s_t} + \alpha_{1,s_t}rsr_{t-1} + \alpha_{2,s_t}rsr_{t-2} + \alpha_{3,s_t}D_t + \varepsilon_t$, where rsr is real silver log-returns.

Figure A1. Data Plot of Real Gold Log>Returns

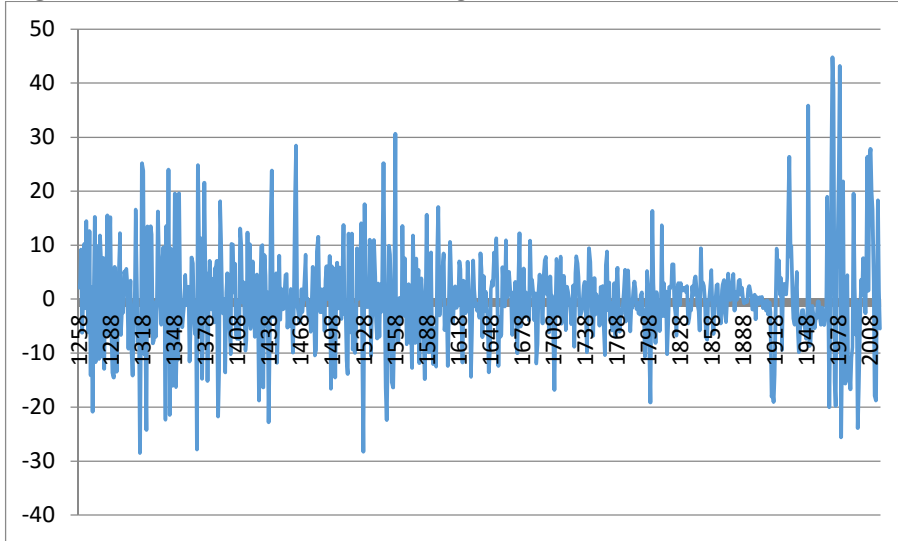
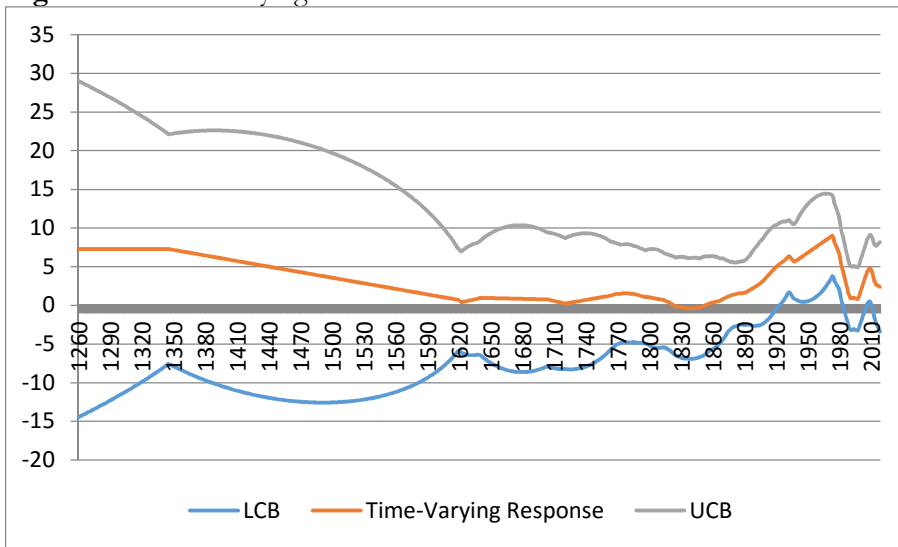


Figure A2. Time-Varying Estimation



Note: LCB and UCB are upper and lower confidence bands respectively for the time varying response of real gold returns to crises.