Forecasting Oil and Stock Returns with a Qual VAR using over 150 Years of Data
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December 2015
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Abstract

The extant literature suggests that oil price, stock price and economic activity are all endogenous and the linkages between these variables are nonlinear. Against this backdrop, the objective of this paper is to use a Qualitative Vector Autoregressive (Qual VAR) to forecast (West Texas Intermediate) oil and (S&P500) stock returns over a monthly period of 1884:09 to 2015:08, using an in-sample period of 1859:10-1884:08. Given that there is no data on economic activity at monthly frequency dating as far back as 1859:09, we measure the same using the NBER recession dummies, which in turn, can be easily accommodated in a Qual VAR as an endogenous variable. In addition, the Qual VAR is inherently a nonlinear model as it allows the oil and stock returns to behave as nonlinear functions of their own past values around business cycle turning points. Our results show that, for both oil and stock returns, the Qual VAR model outperforms the random walk model (in a statistically significant way) at all the forecasting horizons considered, i.e., one- to twelve-months-ahead. In addition, the Qual VAR model, also outperforms the AR and VAR models (in a statistically significant manner) at medium- to long-run horizons for oil returns, and short- to medium-run horizons for stock returns.

JEL Classifications: C32, C53, C55, E32, G10, G17, Q41

Keywords: Vector Autoregressions, Business Cycle Turning Points, Forecasting, Oil and Stock Prices

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1. Introduction

Following the seminal work of Hamilton (1983), a large literature exists that connects movements (in-sample and out-of-sample) in oil prices with recessions in the US economy, a detailed review of which can be found in Hamilton (2011), Balcilar, Gupta, and Wohar (2015), and Baumeister and Kilian (2015). According to Hamilton (2008), nine of ten recessions in the US since World War II have been preceded by an increase in oil price. In fact, Hamilton (2009) even goes so far as to argue that a large proportion of the recent downturn in the US during the “Great Recession” can also be attributed to the oil price shock of 2007-2008. In the same vein, there is also a large literature that links movement in stock prices (again within and out-of-sample) with economic activity, dating as far back as Mitchell and Burns (1938). More recent studies followed, like Estrella and Mishkin (1998), Stock and Watson (2003), Rapach and Weber (2004) Nyberg (2011), and have been surveyed in detail in Balcilar, Gupta and Wohar (2015) and Erdogan et al., (2015).

While, the general belief is that oil and stock prices are leading indicators of the economy, there is ample evidence that economic activity too plays a crucial role in predicting both in and out-of-sample movements in oil (see for example, Kilian (2009), Kilian and Vigfusson (2013), Baumeister and Kilian (2014, 2015) and Baumeister et al., (2015)) and stock prices (see for example, Rapach, Wohar and Rangvid (2005), Goyal and Welch (2008), Rapach, Strauss and Zhou (2010), Rapach and Zhou (2013)). More importantly, as highlighted, amongst others, by Baumeister et al., (2010), Kilian and Vigfusson (2011), Baumeister and Peersman (2013), Balcilar, Gupta and Miller (2015), Bjørnland and Larsen (2015) for the oil market, and Simo-Kengne et al., (2015), Tiwari et al., (2016) and Antonakakis et al., (forthcoming) for the stock market, these relationships with economic activity are in fact nonlinear.

At the same time, there also exists a huge literature, as discussed in Kilian and Park (2009), Apergis and Miller (2009), and Balcilar, Gupta and Wohar (2015), that relates (short and long-run) movements in oil and stock markets through various, somewhat, direct channels (cash-flow, investment, interest rate and exchange rate), and also indirectly through their respective effects on
economic activity. Again, this relationship between oil and stock markets is shown to be characterized more appropriately in a nonlinear fashion rather than a linear one (see for example, Antonakakis and Filis (2013), BalciHar and Ozdemir (2013), Antonakakis, et al., (2014), Boradstock and Filis (2014), Narayan and Gupta (2015), and Kang et al., (forthcoming)). In sum then, oil price, stock price and economic activity are in general related endogenous to each other, with this relationship being more nonlinear than linear.

Against this backdrop, the objective of our paper is to forecast nominal Standard and Poor’s 500 (S&P 500) stock returns and nominal West Texas Intermediate (WTI) crude oil returns over the monthly period of 1884:08-2015:08, based on an in-sample period of 1859:10-1884:07, using a Qualitative Vector Autoregressive (Qual VAR) model. The forecasting performance of the Qual VAR model is compared with random walk and autoregressive (AR) models of oil and stock returns considered separately, and a standard Vector Autoregressive (VAR) model comprising of oil and stock returns. Note that the in- and out-of-sample splits are statistically determined based on multiple structural break tests of Bai and Perron (2003), to ensure that all the breaks are restricted to the out-of-sample period, over which the models are recursively estimated. The recursive estimation allows us to accommodate for parameter changes in the models due to structural breaks.

The Vector Autoregressive (VAR) model, proposed by Sims (1980), though atheoretical, has been shown to forecast macroeconomic and financial variables exceptionally well when compared to various other econometric models (Dueker, 2005; Dueker and Assenmacher-Wesche, 2010; Banbura et al., 2010; Giannone et al., 2015). The VAR is essentially a linear system of equations, whereby in a specific equation, a specific variable is regressed on the past values of itself and past values other variable(s) in this system, with possible allowance for deterministic terms (e.g., constant and trend). In other words, in a VAR all variables comprising it are endogenous. However, one criticism of the VAR forecasting is that
variables in the model tend not to behave as linear functions of their own past values around business cycle turning points.

But, as discussed in the earlier part of this introduction, there is ample evidence that the relationship between oil returns, stock returns and economic activity is nonlinear. Given this, a linear VAR model is, at least theoretically, not suitable for our cause. In this regard, the Qual VAR model, developed by Dueker (2005), helps us in two ways: First, the Qual VAR is essentially a regime-switching (hence, nonlinear) VAR model, based on the idea that the regime is determined by an observed qualitative response variable that is modeled simultaneously within the VAR. Models of this form consider a qualitative variable that is binary, and hence has two regimes such as the state of the business cycle. The advantage of this approach is that it allows one to understand which economic forces drive the regime switches. Second, given that there is no available data on monthly economic activity (like industrial production), dating as far back as 1859:10, the Qual VAR model allows us to use the recession dummies (available at monthly frequency from), which are converted to an underlying continuous variable, to capture economic activity of the US economy.\textsuperscript{1} In the process, our Qual VAR model, over and above the stock and oil returns, includes a truncated normal latent business cycle index that is negative during NBER recessions and positive during expansions. It must be pointed out that while, nonlinearity between oil returns, stock returns, and a measure of economic activity (if available) could be modelled using other nonlinear approaches\textsuperscript{2} like the Markov-Switching VAR (originally developed by Hamilton (1989) in an univariate set-up), smooth threshold VAR (Leamer and Potter, 2002), and time-varying VAR (Primiceri, 2005), the fact that there is no data on economic activity over the

\textsuperscript{1}US industrial production data at monthly frequency only starts from January of 1919. While real GDP data is available from 1800, it is only available at annual frequency. A quarterly real GNP series starting in 1875:1 could be constructed by merging data from the NBER prior to 1947, and then from the FRED database of the Federal Reserve Bank of St. Louis.

\textsuperscript{2}For a detailed discussion in this regard, the reader is referred to Balcilar et al., (2015).
sample period under consideration, tilts the balance, understandably, in favor of the Qual VAR model. This long-sample used by us is also an unique feature of the paper, as it essentially runs from the beginning of the modern era of the petroleum industry with the drilling of the first oil well on August 27, 1859 in Titusville, Pennsylvania.

Note that, to accommodate the problem of overparametrization (often leading to poor forecasts) in the VAR and the Qual VAR when compared to the standard AR, we use Bayesian shrinkage to ensure that all these models have the same in-sample fit and hence, a fair out-of-sample comparison, following the suggestions of Banbura et al., (2010). To the best of our knowledge, this is the first attempt to develop and forecast oil and stock returns with a Qual VAR, using data that spans over 150 years of history of these two important markets.\(^3\) Related research involving forecasting of macroeconomic variables with Qual VARs can be found in Dueker (2005), Dueker and Assenmacher-Wesche (2010), and Gupta et al., (2015). Using a Qual VAR model comprising of output, prices, interest rates, and the term spread (difference between the 10-year government bond yield and the 3-month Treasury bill rate), over and above a latent business cycle index, Dueker (2005) show that the US recession of March, 2001 could have been predicted with great success. Using the same framework, Dueker and Assenmacher-Wesche (2010) finds that the Qual VAR improves on out-of-sample forecasts from a standard VAR for, output, prices, interest rates and the term-spread. Building on this line of work, more recently, Gupta et al., (2015) develop a Factor-Augmented Qual VAR (FA-Qual VAR), where the model include information from a large data set in form of factors. The authors show that the FA-Qual VAR model outperforms the Qual VAR model of Dueker (2005), and Dueker and Assenmacher-Wesche (2010) at short to medium-run horizons when forecasting output, prices, interest rates and the term spread. Though not for forecasting, the Qual VAR approach has also been used to analyse causality

\(^3\) For detailed discussion of the literature on forecasting oil and stock prices (returns), the reader is referred to the studies of Huntington et al., (2013) and Rapach and Zhou (2013) respectively.
between interest rates and state of the business cycle (Nyberg, 2013), and the impact of unconventional monetary policy (Meinusch and Tillmann, forthcoming; Tillmann; 2015, forthcoming).

The remainder of the paper is organized as follows: Section 2 presents a brief description of the Qual VAR model. Section 3 describes the data and presents the results from the forecasting exercise. Finally, section 4 concludes.

2. The Qualitative Vector Autoregressive (Qual VAR) Model

Suppose we observe a qualitative variable, \( y \in \{0,1\} \), which is driven by a continuous latent variable, \( y^* \), such that:

\[
y_t = 0 \text{ if } y_t^* \leq 0
= 1 \text{ if } y_t^* > 0
\]

along with:

\[
y_t^* = \Psi(L)y_{t-1}^* + \Gamma(L)X_{t-1} + \epsilon_t \\
\epsilon \sim N(0,1),
\]

where \( X_{t-1} \) is a set of explanatory variables (oil and stock returns in our case), and \( \Psi(L) \) and \( \Gamma(L) \) are lag polynomials. The qualitative data used for \( y_t \) are the recession/expansion classifications designated by the business cycle dating committee at the NBER. Then, as described in Dueker (2005) and Dueker and Assenmacher-Wesche (2010), a Qual VAR model with \( k \) variables and \( p \) lags is expressed as a standard VAR:

\[
\Phi(L)Y_t = \epsilon_t
\]

with \( \epsilon \sim \text{Normal}(0,\Sigma) \), and where \( Y_t \) is a \( k \times 1 \) vector consisting of oil and stock returns, \( X_t \), plus the latent business cycle turning point index \( y^* \); \( \Phi(L) \) is a set of \( k \times k \) matrices from \( L = 0,\ldots,p \), with the identity matrix at \( L = 0 \), i.e., the VAR regression coefficients are given in \( \Phi(L) \). The parameters that require conditional distributions for Markov Chain Monte Carlo (MCMC) estimation are \( \Phi, y^* \) and \( \Sigma \) (i.e., the covariance matrix), which in turn,
involves a sequence of draws from the following conditional distributions, where superscripts indicate the iteration number:

VAR coefficients ~ Normal

\[ f \left( \Phi^{(i+1)} \right) \left( y_t^{*(i)} \right)_{t=1,\ldots,T}, \{X_t\}_{t=1,\ldots,T}, \Sigma^{(i)} \) (4) \]

Covariance matrix ~ inverted Wishart

\[ f \left( \Sigma^{(i+1)} \right) \left( y_t^{*(i)} \right)_{t=1,\ldots,T}, \{X_t\}_{t=1,\ldots,T}, \Phi^{(i)} \) \]

Latent variable ~ truncated Normal

\[ f \left( y_t^{*(i+1)} \left| \Phi^{(i+1)} \right., \Sigma^{(i+1)} \right\{y_t^{*(i+1)} \}_{j<t}, \left. \{y_k^{*(i)} \}_{k>t}, \{X_t\}_{t=1,\ldots,T} \right) \] (6)

Conditional on a set of values for \( y^* \), \( \Phi \) are normally distributed. While, \( \Sigma \) is part of a normal-inverted Wishart conjugate pair with \( \Phi \). Finally, each observation of \( y^* \), has a truncated normal distribution, where it is not allowed to be negative (positive) during expansions (recessions). Further details on these conditional distributions and prior distributions can be found in the Appendix of Dueker and Assenmacher-Wesche (2010).

3. Data and Forecasting Results

Our data set includes nominal values of the S&P 500 index and WTI Crude oil price, covering the monthly period of 1859:09 to 2015:08. The raw data comes from the Global Financial database, which we seasonally adjust using the X-13 procedure of the US Census Bureau. Note that the MCMC approach of the Qual VAR requires that the data be stationary; hence, we work with nominal stock and oil returns (i.e., the first-differences of the natural logarithms of stock and oil prices expressed in percentages). The Data transformation implies that our effective sample starts from 1859:10-2015:08, with the end date and the starting point being driven purely by data availability at the time of writing this paper. Note that, the qualitative variable is a binary 0/1 variable that denotes recessions and expansions, with
switches taking place at business cycle turning points. The recession and expansion classification comes from the NBER, the information of which is available at: http://www.nber.org/cycles.html.

To determine the in-sample out-of-sample split, we first estimate a VAR model comprising of oil and stock returns and determine the optimal lag-length based on the Akaike Information Criterion (AIC). The AIC suggested 5 lags. We then test for structural breaks in stock returns and the oil returns equations of the VAR(5) using the multiples structural break tests of Bai and Perron (2003). The oil returns equation picked up five breaks at: 1884:08, 1907:11, 1931:09, 1956:12, and 1986:04, while the stock returns equation showed only one break at 1933:06. Given that for the VAR(5) system as a whole, the earliest break was obtained at 1884:08, we chose an in-sample period of 1859:10 to 1884:07. Over the out-of-sample period of 1884:08-2015:08, the models are recursively estimated to produce forecasts at horizons \(h\) of one-month-ahead to twelve-months-ahead.

At this stage, it is important to provide more details on the structure of our pseudo out-of-sample forecasting exercise for the Qual VAR. Keeping the lag-length of the VAR comprising of the stock and oil returns along with the recession/expansion dummy, fixed at 5, we extract the corresponding underlying latent business cycle indicator in a recursive way by adding one observation at a time over the out-of-sample period (1884:08-2015:05) for the variables of interest and the qualitative variable. This is an attempt to replicate a real-life situation that a forecaster faces, whereby the forecaster at the time of generating the first forecast, only has data available till 1884:07, i.e., the end-point of the in-sample. For this purpose, following Dueker and Assenmacher-Wesche (2010), for each recursive estimation over the out-of-sample period, we use 1200 iterations from which the first 300 are discarded to allow for convergence towards the posterior distribution. Figure 1 plots the latent business cycle indicator generated by the Qual VAR. As can be seen, the latent
business cycle indicator picks up the various recessionary periods with great accuracy. Relatively deep recessions are picked up for the “Great Depression”, the oil price shock of 1973, and the recent “Great Recession”. Finally, the AR(5), standard VAR(5), and the Qual VAR (5) are now estimated recursively over the out-of-sample period to produce the forecasts at $h = 1, 2, 3, \ldots, 12$. Note that we can only conduct a pseudo real-time forecasting analysis when a business cycle indicator is involved, since there is considerable time lag with which the NBER releases information that a turning point has occurred. Our data-vintage corresponds to 2015:09.

An additional point that needs to be discussed now is the issue of overparameterization in the VAR and the Qual VAR relative to the AR. To address this concern, we impose the standard Minnesota prior, as developed by Litterman (1986), on the parameters of the VAR and the Qual VAR. The Minnesota prior imposes restrictions on the coefficients of longer lags by assuming that these are more likely to be near zero than the coefficient on shorter lags. However, if there are strong effects from less important variables, the data can override this assumption. The restrictions are imposed by specifying normal prior distributions with zero means and small standard deviations for all coefficients with the standard deviation decreasing as the lags increases. The exception to this, however, is the coefficient on the first own lag of a variable, which has a mean of unity. But, if the variables in the VAR are stationary (which happens to be in our case), one needs to also impose a zero prior mean on the coefficient of the first own lag of a variable. The reader is referred to Litterman (1986) and Banbura et al., (2010) for the technical details, which is quite well-known in the forecasting literature now, and hence has been omitted from the discussion here. In the Minnesota prior-settings, a hyperparameter is used to determine how prior beliefs relate to the information contained in the data. More precisely, this hyperparameter controls the overall tightness of the prior distribution around the prior
mean. Banbura et al., (2010), argue that this tightness-hyperparameter should reflect the size of the system, i.e., as the number of variables increases, the parameters should shrink to avoid overfitting. This, in turn, is achieved by setting this hyperparameter to match the in-sample fit as the benchmark AR models of oil and stock returns. Understandably, the AR models have an infinite value for this hyperparameter with the corresponding values for the VAR and Qual VAR being 0.0821 and 0.0712, and 0.1757 and 0.0807 for the cases of oil returns and stock returns respectively. These values of the hyperparameter in turn, ensures an in-sample fit of 0.2947 and 0.3887 – as obtained for the AR models of oil and stock returns respectively.

Table 1 presents the forecasting results for oil and stock returns at $h=1, 2, 3, \ldots, 12$ emanating from the AR, VAR, and the Qual VAR. The entries corresponding to the Qual VAR for each variable are MSFE of the Qual VAR relative to the Random Walk (RW) model with drift. Hence a value less than one is indicative of the superior forecasting performance of the Qual VAR in comparison to the RW model, which in turn, is found to be the case for both oil and stock returns at all horizons. Entries corresponding to AR and VAR for both variables are MSFE of the AR and VAR relative to the Qual VAR model.\(^4\) Thus, in cases where these values are greater than one, it indicates that the Qual VAR outperforms the AR and VAR. As can be seen from Table 1, for oil returns, this is consistently the case at medium- to long-run horizons, i.e., $h=5$ to 12 when compared to the AR, and for $h=6$ to 12 relative to the VAR. For the case of stock returns, the scenario is reversed in terms of horizons, with the Qual VAR outperforming the AR and VAR models for short- to medium-run horizons, i.e., for $h=1$ to 8. For the horizons where the Qual VAR is not the best performing model, the evidence is slightly mixed in terms of the superior forecasting model. More specifically, for oil returns the AR model outperforms the VAR at $h=1$, but for $h=2$ to 5, the VAR is the best model.

\(^4\) It is easy to deduce from these ratios that the AR and VAR also outperform the RW model for $h=1\ldots12$, just like the Qual VAR does.
For stock returns, the AR is the best model for $h=9, 10$ and $12$, while the VAR outperforms the AR at $h=11$.

Note that the Qual VAR nests all the other models, i.e., the RW, AR and VAR. Given this, we use McCracken’s (2007) powerful $MSE-F$ test statistic to determine whether the scenarios in which the Qual VAR outperforms the other models are significant or not. As indicated by the bold entries in the table, the $MSE-F$ statistic is significant at the 5 percent level for all the cases where it outperforms the RW, AR and VAR for both oil and stock returns. So considering the performance of the Qual VAR, our results highlight the statistical importance of modeling nonlinearity through the use of the latent business cycle indicator at short- to medium-run horizons for stock returns, and medium- to long-run forecast steps for the oil returns.

4. Conclusions

There exists a vast literature on the interrelationships between oil price, stock price and economic activity in the US (as well as the world). Reading of the literature tends to suggest that there are causal relationships running both ways amongst these three variables (i.e., these variables are all endogenous to each other), and these relationships are nonlinear in nature. Against this backdrop, the objective of this paper is to use a Qualitative Vector Autoregressive (Qual VAR) to forecast West Texas Intermediate oil and S&P500 stock returns over a monthly period of 1884:09 to 2015:08, using an in-sample period of 1859:10-1884:08, with this split being determined by tests of multiple structural breaks. The unique feature of our data set is that it covers the entire modern era of the oil industry, given that first oil in the US was drilled in 1859:08 in Titusville, Pennsylvania. The Qual VAR helps us in two ways: (i) Given that there is no data on economic activity at monthly frequency dating as
far back as 1859:09, we measure the same using the NBER recession dummies, which in turn, can be easily accommodated in a Qual VAR as an endogenous variable, unlike in a standard VAR; and, (ii) The Qual VAR is inherently a nonlinear model as it allows the explanatory variables in it to behave as nonlinear functions of their own past values around business cycle turning points – again something not possible in the standard VAR model, but is important for our purpose, given that the literature suggests that, oil price, stock price and economic activity are related in a nonlinear fashion.

Our results show that the Qual VAR model outperforms the random walk (RW) model for one- to twelve-months-ahead forecasts for both oil and stock returns. In addition, when we compare the Qual VAR model with AR and VAR models, we observe the following: (i) For oil returns, the Qual VAR consistently in a statistically significant manner, outperforms the AR and VAR models at at medium- to long-run horizons, i.e., forecast horizons \( h = 5 \) to \( 12 \) when compared to the AR, and for \( h = 6 \) to \( 12 \) relative to the VAR; and, (ii) For the case of stock returns, the Qual VAR outperforms the AR and VAR models in a statistically significant way, for short- to medium-run horizons, i.e., for \( h = 1 \) to \( 8 \). So considering the performance of the Qual VAR, our results highlight the importance of modelling nonlinearity through the use of the latent business cycle indicator when forecasting oil and stock returns, especially at medium- to long-run horizons for the former and short- to medium-run horizons for the latter. As part of future research, given that the VAR and Qual VAR are estimated using Bayesian methods, we can analyse the whole distribution of the forecasts for oil and stock returns.
References


Table 1. Forecasting results from AR, VAR and Qual VAR: 1884:08-2015:08

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Note: Entries corresponding to Qual VAR for each variable are MSFE of the Qual VAR relative to the Random Walk (RW) model; Entries corresponding to AR and VAR for each variable are MSFE of the AR and VAR relative to the Qual VAR model. Entries in bold indicates significance of McCracken’s (2007) MSE-F statistic at the 5 percent level.
**Figure 1.** Plot of the Latent Business Cycle indicator from the Qual VAR: 1859:10-2015:08

Note: CYCLE stands for NBER recession dates, and YSTAR stands for the latent continuous business cycle indicator ($y^*$).