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Aviral Kumar Tiwari

Montpellier Business School

Juncal Cunado

University of Navarra

Rangan Gupta

University of Pretoria

Mark E. Wohar

University of Nebraska at Omaha and Loughborough University

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Department of Economics  
University of Pretoria  
0002, Pretoria  
South Africa  
Tel: +27 12 420 2413

# Are Stock Returns an Inflation Hedge for the UK? Evidence from a Wavelet Analysis Using Over Three Centuries of Data

Aviral Kumar Tiwari<sup>♦</sup>, Juncal Cunado<sup>\*</sup>, Rangan Gupta<sup>^</sup> and Mark E. Wohar<sup>\*</sup>

## Abstract

This paper analyzes the relationship between stock returns and the inflation rates for the UK over a long time period (February 1790 to February 2017) and at different frequencies, by employing a wavelet analysis. We also compare the results for the UK economy with those for the US and two developing countries (India and South Africa). Overall, our results tend to suggest that, while the relationship between stock returns and inflation rates varies across frequencies and time periods, there is no evidence of stock returns acting as an inflation hedge, irrespective of whether we look at the two developed or the two developing markets in our sample.

**Keywords:** nominal and real stock returns, inflation, frequency-domain, wavelet analysis.

**JEL Codes:** C49, E31, G12.

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<sup>♦</sup> Center for Energy and Sustainable Development (CESD), Montpellier Business School, Montpellier, France, Email: [aviral.eco@gmail.com](mailto:aviral.eco@gmail.com).

<sup>\*</sup> University of Navarra, School of Economics, Edificio Amigos, E-31080 Pamplona, Spain. Email: [jcunado@unav.es](mailto:jcunado@unav.es).

<sup>^</sup> Department of Economics, University of Pretoria, Pretoria, 0002, South Africa. Email: [rangan.gupta@up.ac.za](mailto:rangan.gupta@up.ac.za).

<sup>\*</sup> Corresponding author. College of Business Administration, University of Nebraska at Omaha, 6708 Pine Street, Omaha, NE 68182, USA; and School of Business and Economics, Loughborough University, Leicestershire, LE11 3TU, UK. Email: [mwohar@unomaha.edu](mailto:mwohar@unomaha.edu).

## 1. Introduction

While the 19th century was characterized by periods of moderate inflation and deflation in the UK (between 1790 and 1914, a period of over a century, prices were at about the same level), the evolution of inflation in the 20th and the beginning of the 21st centuries has been very different. First, as far as the inflation trend is concerned, since the First World War, prices have increased more than forty-fold (O'Donoghue et al., 2004). Second, the period can be divided into a number of episodes of deflation (such as the interwar instability period from 1924-1939; the Bretton Woods and the Dollar Standard period from 1949-1970; or, the relatively more stable decades from 1980 to 2000) and inflation (the period after World War I, from 1914-1924; the World War II and postwar period, from 1939-1949; or, the oil price crisis period from 1973 to 1981, when prices more than tripled, with inflation reaching 24% in 1975, and exceeding 10% in each year except 1978)<sup>1</sup>, showing the great heterogeneity in the inflation rate behavior over these years. Inflation rates have always been a key variable of interest, and its stabilization constitutes one of the objectives of the UK monetary policy. Although inflation decreases the value of money, according to the generalized Fisher hypothesis (Fisher, 1930), in an efficient market, investors should be fully compensated for the increased price levels with an increase in nominal stock returns, so that real stock returns should only reflect expectations about real factors. This implies that real stock returns and inflation should vary independently, that is, stock returns should serve as a hedge against inflation, and, if this theory holds, we should observe a positive and one-to-one relationship between nominal stock returns and inflation rates. On the other hand, a positive relationship between nominal stock returns and inflation rates could also be explained by the Wealth Effect Hypothesis (Ando and Modigliani, 1963), since real stock returns can impact inflation

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<sup>1</sup> See O'Donoghue et al. (2004) for a detailed description of inflation in the UK since 1750.

rates through their effect on consumption and hence aggregate demand. According to this theory, there are different channels through which stock prices can affect consumption (see, for example, Ludwig and Sløk, 2004 and Simo-Kengne et al., 2015), such as the realized gain, the expectation that raising the current stock price will result in higher future income and wealth, the liquidity constraint effect and the stock option value effect. Based on these two theories (Fisher Effect and Wealth Effect), a positive relationship between nominal stock returns and inflation rates should be observed in the data.

The empirical relationship between (nominal and real) stock returns and inflation has also been extensively analyzed in the literature, and many of papers have found a negative correlation between real stock returns and inflation, rejecting, the Fisher and the Wealth Effect hypotheses (Lintner, 1975; Bodie, 1976; Fama and Schwert, 1977; Fama, 1981; Gertler and Grinols, 1982; Barsky, 1987; Kaul, 1987; Kaul and Seyhum, 1990). Thus, several theories alternatives to the Fisher Hypothesis have emerged in the literature to try to explain the negative correlation between real stock returns and inflation. For example, Modigliani and Cohn (1979) hypothesizes that stock market investors fail to understand inflation's effect on the nominal cash flow, and in the presence of sustained inflation the valuation errors will induce an undervaluation of stocks – the Money Illusion Hypothesis. Feldstein (1980) argues that sustained increases in inflation reduces real stock prices since the artificial capital gains due to inflation will increase corporate tax liabilities and will reduce real after-tax earnings – the Tax Effect Hypothesis. Fama (1981) shows that the negative relationship between real stock returns and expected inflation is generated by a positive relationship between the stock market and economic activity and the negative correlation between inflation and real activity – the Proxy Effect Hypothesis. Geske and Roll (1983) suggest that stock price's reaction is in anticipation of future economic activity and is highly correlated to government revenues. When economic output decreases and the government faces a deficit, the Treasury either

borrowers or issues money, causing inflation. Thus, stock returns and inflation are negatively related due to a fiscal and monetary linkage – the Reverse Causality Hypothesis-. It is clear that, there are many theories which try to explain the relationship between stock returns and inflation rates, with very different empirical implications. Policy implications will also be very different depending on the theory used to explain the connection between these two variables.

Empirical evidence on these hypothesis has been mixed, although most empirical studies that reject the Fisher hypothesis have examined the relationship between inflation and stock returns at shorter horizons (Lintner, 1975; Bodie, 1976; Fama and Schwert, 1977; Fama, 1981; Gertler and Grinols, 1982; Kaul, 1987; Kaul and Seyhum, 1990; Hess and Lee, 1999), while, as the horizon increases, the results are more likely to support the Fisher hypothesis (Boudoukh and Richardson, 1993; Solnik and Solnik, 1997; Schotman and Schweitzer, 2000; Lothian and McCarthy, 2001). Lothian and McCarthy (2001), for example, find that equities are an inflation hedge, although this is only the case over very long periods. Cagan (1974) also finds that equity markets did adjust to inflation, but that the adjustment period lasted more than a decade. Two empirical results found in this literature are worth mentioning. First, some papers show that the sign and strength of the correlation between stock returns and inflation depend on the frequency scale. For example, Kim and In (2005), applying a wavelet analysis, show that there is a positive relationship between stock returns and inflation at the shortest scale (1-month period) and at the longest scale (128-month period), while a negative relationship is shown at the intermediate scales. Arouri et al. (2014) test for the Fisher hypothesis using data for Pakistan through a wavelets analysis and find that stocks could be used as a hedge against inflation in the long-run. Second, the results reveal that correlations between inflation and stock market returns are evolving heterogeneously overtime (Valcarcel, 2012; Antonakakis et al., 2017). In this paper, we allow

for these two possibilities (different correlation levels between inflation rates and stock market returns at different frequency scales and at different moments in time) by means of using different wavelets transforms for testing whether stock market returns can be considered an inflation hedge in a sample of two developed and two developing countries.

In this context, the objective of this paper is to test whether stock prices can be considered an inflation hedge for the UK economy, using a long span of data which covers observations for over the last three centuries (February 1790-February 2017). Furthermore, we compare the results obtained for the UK with those for the US and two developing countries (India, South Africa). The main contributions of the paper are the following. First, although our primary interest is to analyze the relationship between inflation rates and stock returns in the UK, our sample of countries in the empirical analysis includes two developed countries (the UK and the US) and two emerging countries (India and South Africa). Inflation rates in emerging countries have been higher and more volatile than in developed countries (Mitchell, 1998) and have also been characterized by significant changes over time, including the recent inflation episode due to the commodity price increase in 2007-2008, which mostly affected emerging economies. Furthermore, financial markets in developing countries are less developed and investors have a narrower range of other inflation hedges to choose from than do investors in developed countries. Since all these factors could affect the stock-returns-inflation relationship, we believe that comparing the case of the UK economy with those of two developing countries (India and South Africa) adds an additional importance to our analysis. Second, the analysis covers the time period from February 1790 to February 2017, a period of time in which both stock returns and inflation rates have evolved heterogeneously over time, which suggests that the strength and sign of the relationship between the two variables are likely to have changed over the analyzed period. The nature of this long period makes more appropriate the use of the methodology employed in the paper. Finally, our main

contribution is to examine the relationship between these two variables by means of a wavelet coherency analysis in the time and frequency domains. Wavelet coherency and phase differences simultaneously evaluate how causalities between stock returns and inflation rates fluctuate across frequencies and vary over time. This allows us to obtain short-term (high frequency) and long-term (long-frequency) relationships between the two series, and thus controls for potential nonlinearities and structural breaks in the relationship between the variables. The same methodology was used by Bhanja et al. (2012) to analyze the relationship between these variables in the Indian case, although, to the best of our knowledge, our paper is the first one that uses a wavelet approach to explore the relationship between the stock returns and inflation rates for the UK economy, the US, India and South Africa using over three centuries of data.

As assumed, our main results suggest that inflation rates and nominal stock returns present common movements, especially in the medium- and long-run. The results also confirm that the relationship between the two variables has changed over time during the long sample historical time period considered. Overall, our results tend to suggest that, while the relationship between stock returns and inflation rates varies across frequencies and time periods, there is no evidence of stock prices acting as an inflation hedge, irrespective of whether we look at the two developed or the two developing markets in our sample.

The remainder of the paper is structured as follows. Section 2 describes the methodology. Section 3 presents the data and the main empirical results, while Section 4 contains some concluding comments and policy implications.

## 2. Methodology and data

### 2.1. Methodological aspects

Through wavelets, the correlation levels are assessed at different frequency scales and at different moments in time. Practically, each time series is decomposed in different frequencies and this decomposition can be made using different wavelets transforms (i.e. discrete, continuous, multiple). Our paper relies particularly on the Continuous Wavelet Methodology (CWT) methodology which provides time-frequency evolution of a series under consideration and across all the times and frequencies the coherence structure between stock returns and inflation. This section provides only elementary notions about the CWT methodology (for a detailed description see Torrence and Compo, 1998; Grinsted et al., 2004; Aguiar-Conraria and Soares, 2008; Rua and Nunes, 2009; Tiwari, 2013).

The wavelet transform decomposes a time series in functions (wavelets) localized both in time and frequency  $\psi_{\tau,s}(t)$ . For a discrete time series  $x(t)$ , the CWT is:

$$W_x(\tau, s) = \frac{1}{\sqrt{s}} \sum_{t=1}^N x(t) \psi^* \left( \frac{t-\tau}{s} \right) \quad (1)$$

Torrence and Compo (1998) show that for a discrete time series, the CWT is defined as a convolution and can be efficiently computed as a product in the Fourier space where the Morlet wavelet (with  $\omega_0=6$ ) is a good choice in decomposing a signal.

Consequently, the studies using the wavelet coherence for assessing the co-movements of financial series usually resort to the Morlet wavelet, defined as:

$$\psi(t) = \pi^{-\frac{1}{4}} e^{i\omega_0 t} e^{-\frac{1}{2}t^2} \quad (2)$$

where:  $\omega_0$  is the frequency dimension and  $t$  is the time dimension.

The corresponding Fourier transform is given by:

$$\hat{\psi}(\omega) = \pi^{\frac{1}{4}} \sqrt{2} e^{-\frac{1}{2}(\omega-\omega_0)^2} \quad (3)$$

The wavelet power spectrum (WPS), which shows the variance of the time series (i.e., signals) across time-scale, is defined by  $|W_x(\tau, s)|^2$ , while the white-noise and red-noise wavelet power spectra is (Torrence and Compo, 1998)<sup>2</sup>:

$$D\left(\frac{|W_x(\tau, s)|^2}{\sigma_x^2} < p\right) = \frac{1}{2} P_k \chi_\nu^2(p) \quad (4)$$

where:  $\nu$  is equal to 1 for real and 2 for complex wavelets;  $P_k$  is the mean spectrum at the Fourier frequency  $k$ .

In addition, the wavelet coherence (WTC) method allows the estimation of the presence of a simple cause-effect relationship between the phenomena recorded in the time series. Torrence and Webster (1999) define the WTC of two time series with  $W_x(\tau, s)$  and  $W_y(\tau, s)$  wavelet transforms, as the absolute value squared of the smoothed cross-wavelet spectrum, normalized by the smoothed wavelet power spectra:

$$R^2(\tau, s) = \frac{|S(s^{-1}W_{xy}(\tau, s))|^2}{S(s^{-1}|W_x(\tau, s)|^2) \cdot S(s^{-1}|W_y(\tau, s)|^2)} \quad (5)$$

where:  $S(\cdot)$  is a smoothing operator and  $s$  is the wavelet scale.

However, the CWT suffers from edge effects due to the fact that wavelets are not completely localized in time. Thus, to address this issue, we use the cone of influence (COI). Outside the COI, the edge effects are predominant and can distort the result. Further, the phase relationship is computed using the circular mean of the phase over regions with greater than 5% statistical significance that are outside the COI. The circular mean of a set of angles  $(a_t, t = 1, \dots, n)$  is defined as follows:

$$a_m = \arg(A, B) \quad (6)$$

where:  $A = \sum_{t=1}^n \cos(a_t)$  and  $B = \sum_{t=1}^n \sin(a_t)$ .

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<sup>2</sup> We use the theoretical distribution of the wavelet power spectrum for computing the significance levels.

Further we define the phase difference as follows, which shows any lag or lead relationships between components,

$$\phi_{x,y} = \tan^{-1} \frac{I\{W_n^{xy}\}}{R\{W_n^{xy}\}}, \phi_{x,y} \in [-\pi, \pi] \quad (7)$$

where,  $I$  and  $R$  are the imaginary and real parts, respectively, of the smooth power spectrum. A phase difference of zero indicates that the time series move together (analogous to positive covariance) at the specified frequency; if  $\phi_{x,y} \in [0, \pi/2]$ , the series move in-phase, with the time-series  $y$  leading  $x$ ; if  $\phi_{x,y} \in [-\pi/2, 0]$ , the series move in-phase, with the time-series  $x$  leading  $y$ . We have an anti-phase relation if we have a phase difference of  $\pi$  (or  $-\pi$ ). If  $\phi_{x,y} \in [\pi/2, \pi]$ , there is anti-phase relation with  $x$  leading  $y$  and if  $\phi_{x,y} \in [-\pi, -\pi/2]$ , there is anti-phase relation with  $y$  leading  $x$ .

## 2.2 Data

Our data comprises of monthly nominal and real stock returns and inflation for the UK – our main focus, and then also for two emerging markets (India and South Africa), and a developed market (US). The choice of these countries is based on availability of historical data, and provides a comparison of the results for UK with that of emerging and developed economies. Nominal stock prices are derived from Global Financial Database, and are converted to nominal stock returns by using the first differences of natural logarithms expressed in percentages by multiplying with 100; i.e., we consider log returns. For UK, we use the wholesale/producer price index as a measure of the price level, which in turn, is derived from the Three Centuries of Data (Version 2.3) maintained by the Bank of England at: <http://www.bankofengland.co.uk/research/Pages/datasets/default.aspx>. This data is available till April, 2016. The data is then updated till end of our sample period from International Financial Statistics of the International Monetary Fund. We use this measure of

price level for the UK rather than Consumer Price Index (CPI), since CPI data is only available from 1914.<sup>3</sup> For the remaining three countries used in comparison, we use the CPI as a measure of price level. The CPI data for the India and South Africa are derived from the Global Financial Database. For the US, the data is obtained from the data segment of Professor Robert J. Shiller's website: <http://www.econ.yale.edu/~shiller/data.htm>. Inflation is computed as month on month changes in the natural logarithms of the measure of price level expressed in percentages. Real stock return is then derived by subtracting the inflation rate from the nominal stock returns. Based on data availability the sample of data covered are: 1790:02-2017:02 for UK; 1920:08-2017:02 for India; 1936:01-2017:01 for South Africa; and 1871:02-2017:02 for US. The data on nominal and real stock returns, and inflation have been plotted in Figure A1 in the Appendix of the paper.

### **3. Data analysis and findings**

The results for each country under consideration is presented in Figures 1 to 12 through the wavelet power spectrum (WPS), and its average power spectrum, cross-wavelet transform (XWT) and its average power spectrum, wavelet coherency (WC) and phase-differences. The output of WPS, XWT and WC is illustrated by contour plots arranged in three dimensions: frequency and time spaces (i.e., the vertical and horizontal axes of the contour plots), and the time-scale wavelet spectrum values (i.e., the colored spectrum of increasing intensity from dark blue to red). More specifically, an increasing value of the wavelet spectrum matches up with a deepening red color. The frequency is converted into time units (months), and it ranges from the highest frequency of 2 months (top of the plots) to the lowest frequency of 512 months (bottom of the plots). The time on the horizontal axis indicates the whole sample period for each country under consideration. A significant red color at the extreme left/right

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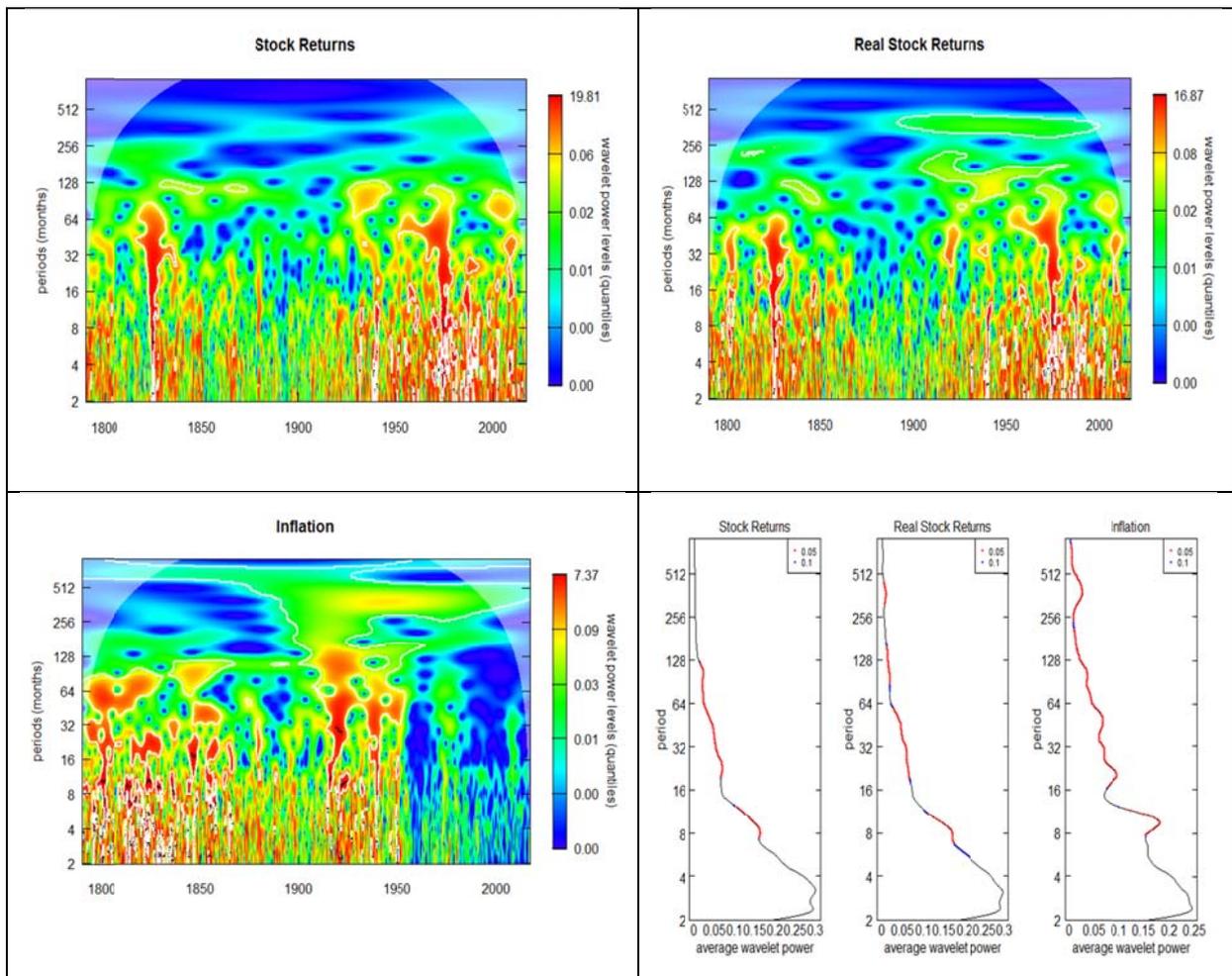
<sup>3</sup> Our results were however, qualitatively similar over the period of 1914:08 to 2017:02 if we used the CPI-based measure of inflation, rather than the wholesale or producer price based inflation. Complete details of these results are available upon request from the authors.

corner indicates the existence of extreme events at the beginning/end of the period, while the same color concentration at the bottom/top implies the occurrence of significant scenarios at low/high frequencies. A visual assessment of the figures shows that both extreme time and frequency movements are detected.

### *3.1. Wavelet analysis for UK*

Since the focus of our paper is the UK, we present the results for UK first and in great details. The WPS (which is sometimes referred as Local Wavelet Power Spectrum (LWPS) in the literature) results for UK is presented in Figure 1 in four parts. In the left-upper corner we present WPS of nominal stock returns and right-upper corner we present results of WPS of real stock returns. Left-lower corner presents the WPS of inflation and left-lower corner presents average wavelet power (also known as Global Wavelet Power Spectrum (GWPS) which gives the averaged variance contained in all wavelet coefficients of the same frequency) of nominal stock returns, real stock returns and inflation respectively. The WPS is helpful in identifying the similarities in the evolution of the data series across time-scale. Without being a direct proof of either co-movements or lead-lag relationships, the results of the WPS can be interpreted as a first sign of interdependences between nominal and real stock returns and inflation.

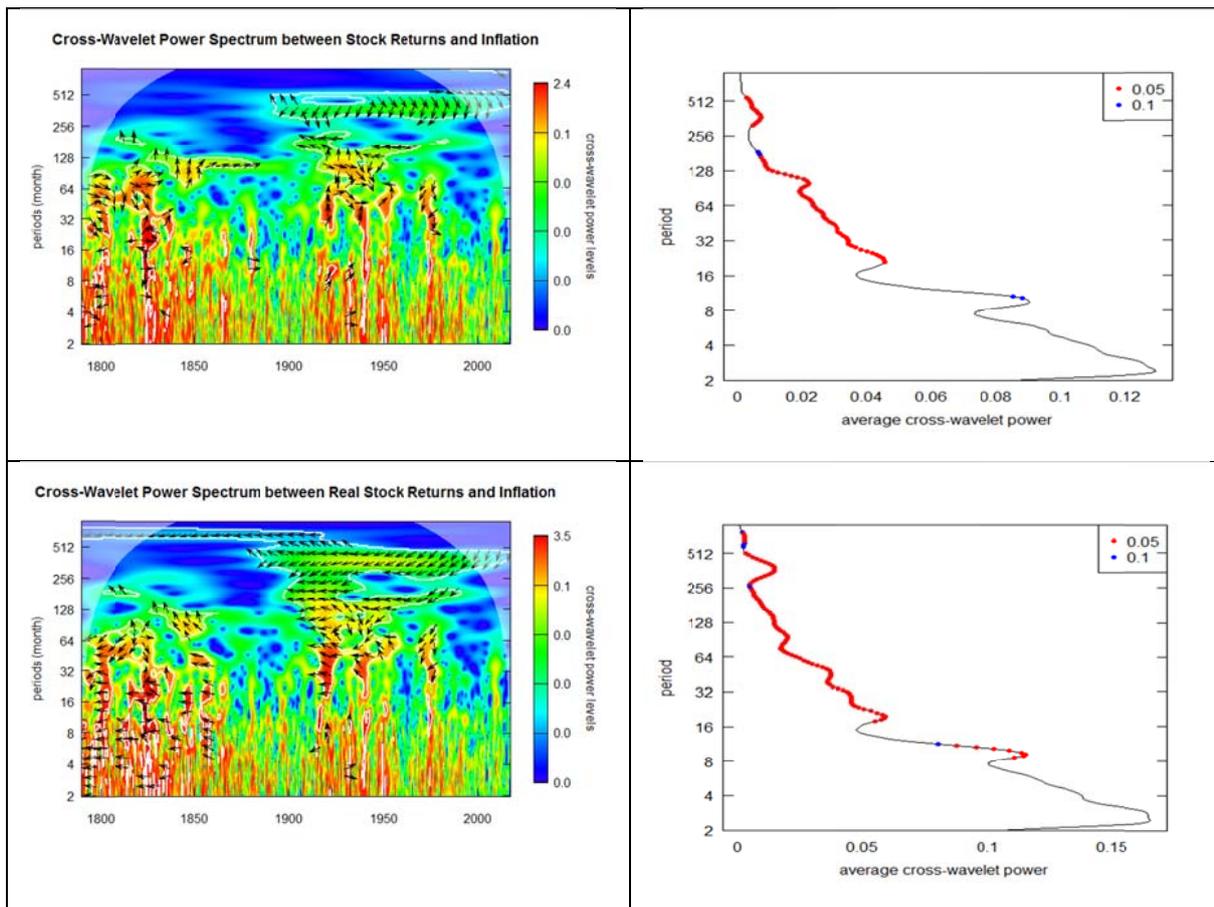
**Figure 1: WPS and average wavelet power for UK**



It is evident from Figure 1 that high wavelet power levels of nominal stock and real stock returns are in the same periods and frequencies. In particular, nominal stock and real stock returns showing high wavelet power levels between the 2 to 64 months scale, represented by red color contour, are around 1800, 1825, and since 1930 till 2016. However, for inflation, the period before 1950 represents high wavelet power in the 2 to 64 months scale. If we analyze the plots of average wavelet power, we find significant (at the 5% level) common months scale of 16 to 128 between nominal stock returns and inflation, and at the 16 to 230 months scale for real stock returns and inflation. To further validate these findings, we use the cross wavelet transform (XWT) and its average power spectrum.

It is very interesting to observe that in Figure 2, in general, the portrayed pattern of average cross-wavelet power is same for both nominal stock returns and inflation, and real stock returns and inflation. If we observe closely, we find that the average cross-wavelet power is consistently significant between the 16 to 512 months range, as well as between the 8 to 10 months scale, when real stock return is analysed with inflation. But for nominal stock returns, the average cross-wavelet power is significant between 16 to 128 months and between 256 and 512 months. In terms of the direction of arrows associated with the cross-wavelet power spectrum, they are not consistent and it is very difficult to draw conclusions, because for same period at different frequencies arrows are pointing right up or down, and left up or down. In other words, the direction of the arrows varies across various frequency bands over the time period under consideration. Even though it is difficult to draw clear-cut conclusions, one can observe a strong link between nominal and real stock returns with inflation as seen from the average cross-wavelet power figures. However, to get more insight about the lead-lag relationship, we now turn to wavelet-coherency and phase-differences, as presented in Figure 3.

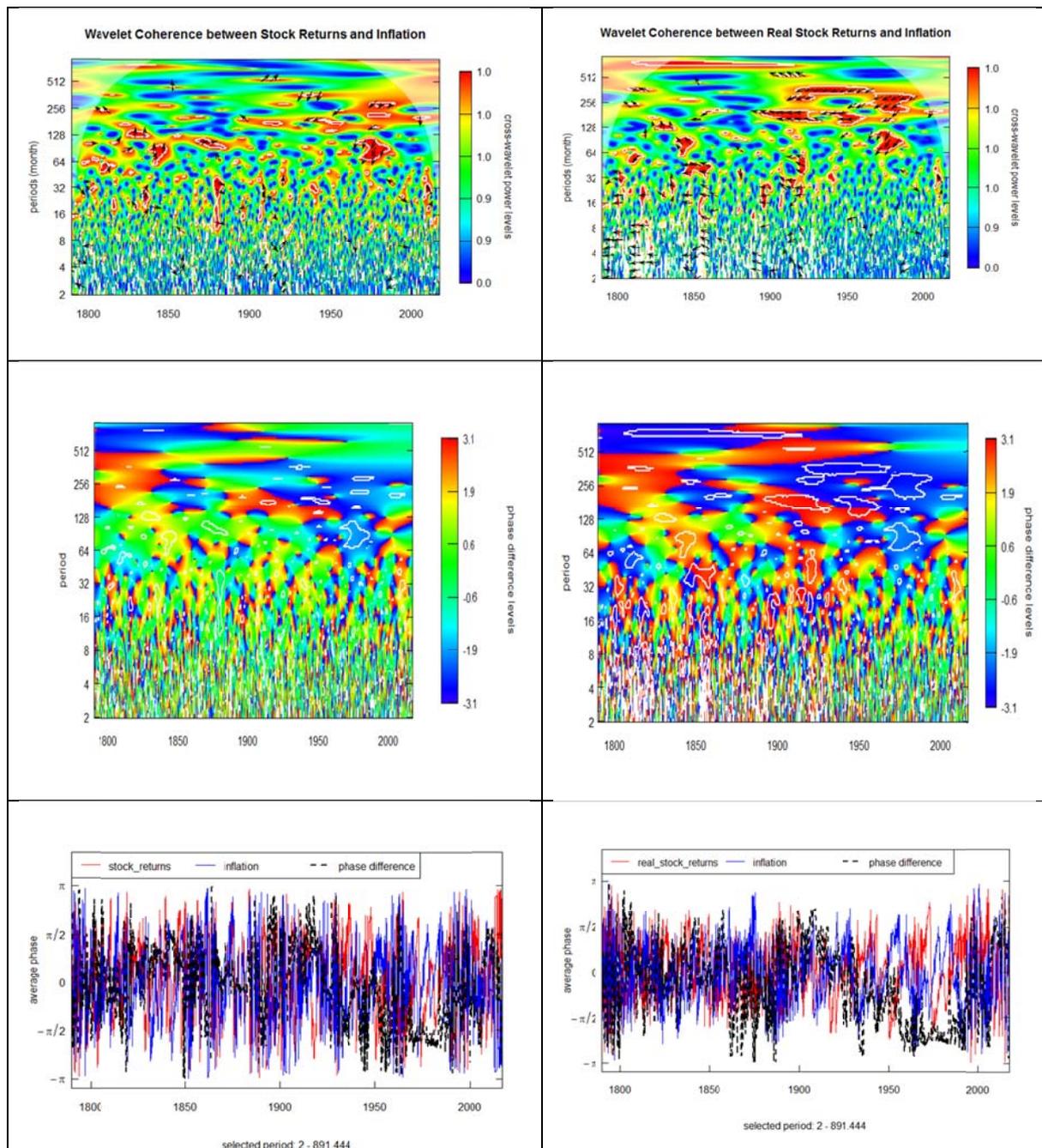
**Figure 2: Cross-Wavelet Transform (XWT) and average wavelet power for UK**



While the WPS offers some insights about the probable co-movements of the series, the wavelet coherence, together with phase-difference, provides not only a good tool for a descriptive analysis of the relationship, but also for examining the co-movements and lead-lag relationships. We document that the variables under consideration depict common movements, especially in the medium- and long-runs. Figure 3 has two columns and three rows, with the first column presenting results for nominal stock returns and inflation, and the second column doing the same for real stock returns and inflation. The first row in Figure 3 depict results of wavelet-coherence (and phase-differences through arrows), a global pattern of average phase difference is graphed in the second row to demonstrate phase-or anti-phase and lead and lag relationship between nominal or real stock returns and inflation, where the color code represents the power of phase difference, with it ranging from  $-3.1$  (i.e.,  $-\pi$ ) (dark

blue color) to 3.1 (i.e.,  $\pi$ ) (dark red color), and finally in the third row, averaged phases and phase-difference are plotted.

**Figure 3: Continuous Wavelet Coherency (CWT) and phase-differences for UK**



Our results based on wavelet-coherency (from the first row of the Figure 3) for both nominal stock returns and inflation, and real stock returns and inflation indicate arrows mostly

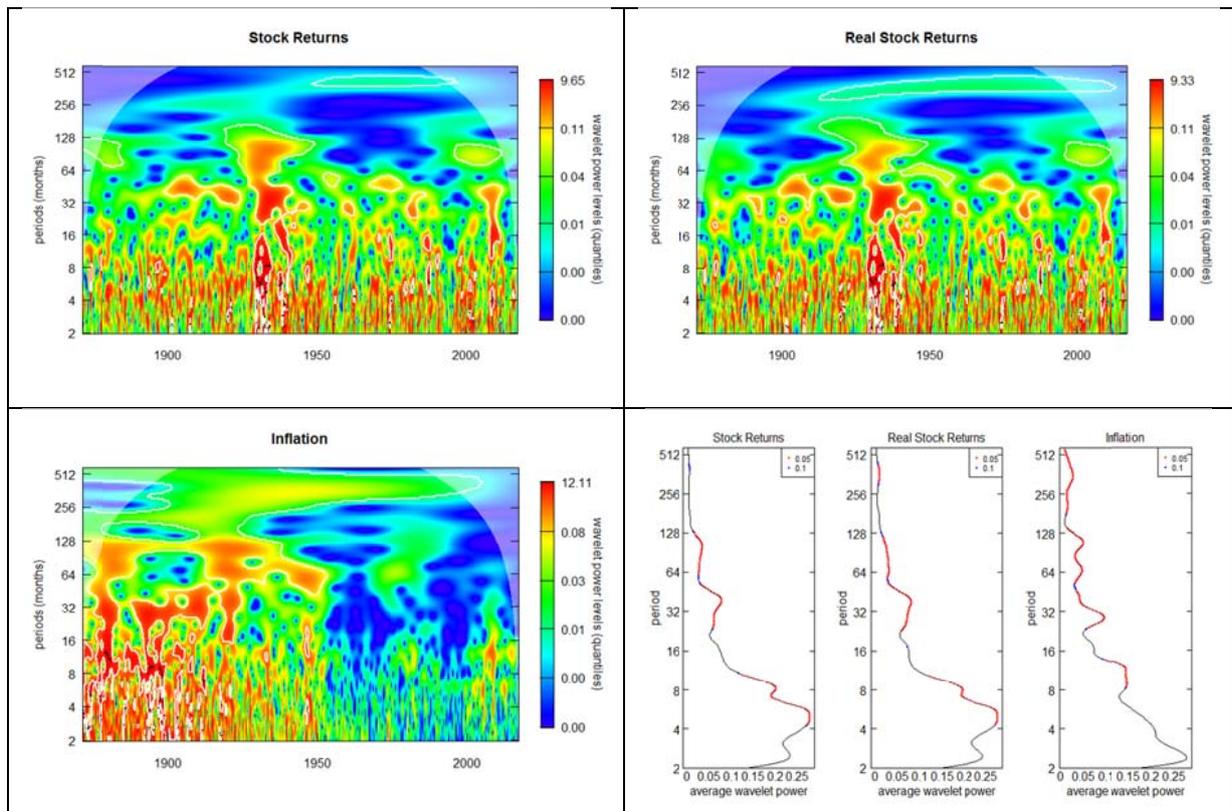
pointing upward-left at the 4~64 months scale over different periods. This implies that inflation and stock returns are out of phase (i.e., anti-cyclical) for most of the periods. Similarly, at more than 128 months scale, especially over the 1920 to 2017 period, inflation and stock returns are out of phase (negative relationship). In the second row of Figure 3, a global pattern of averaged phase difference is presented to demonstrate phase-or anti-phase and lead-lag relationship between stock returns and inflation. But to get a clearer understanding, we analyze the pattern of average phase differences presented in third row of Figure 3. We find that for the period prior to 1800, 1875-1890, and 1950-2000, phase falls mostly between  $[-\pi, -\pi/2]$ , indicating that there is anti-phase relation with inflation leading stock returns. The negative relationship between stock returns and inflation in turn can be due to the Money Illusion, Tax Effect, Proxy Effect, and/or Reverse Causality Hypotheses. During the other periods (1800 to 1870, 1900-1950 and post 2000) inflation and stock returns are in phase  $[\pi/2, -\pi/2]$ , with stock returns leading inflation in general. In other words, evidence in favour of stock returns acting as an inflation hedge is virtually non-existent, even though, we do have episodes of positive relationship between stock returns and inflation, which in turn, are primarily due to the wealth effect.

### *3.2. Comparison with the Wavelet analyses for US, India and South Africa*

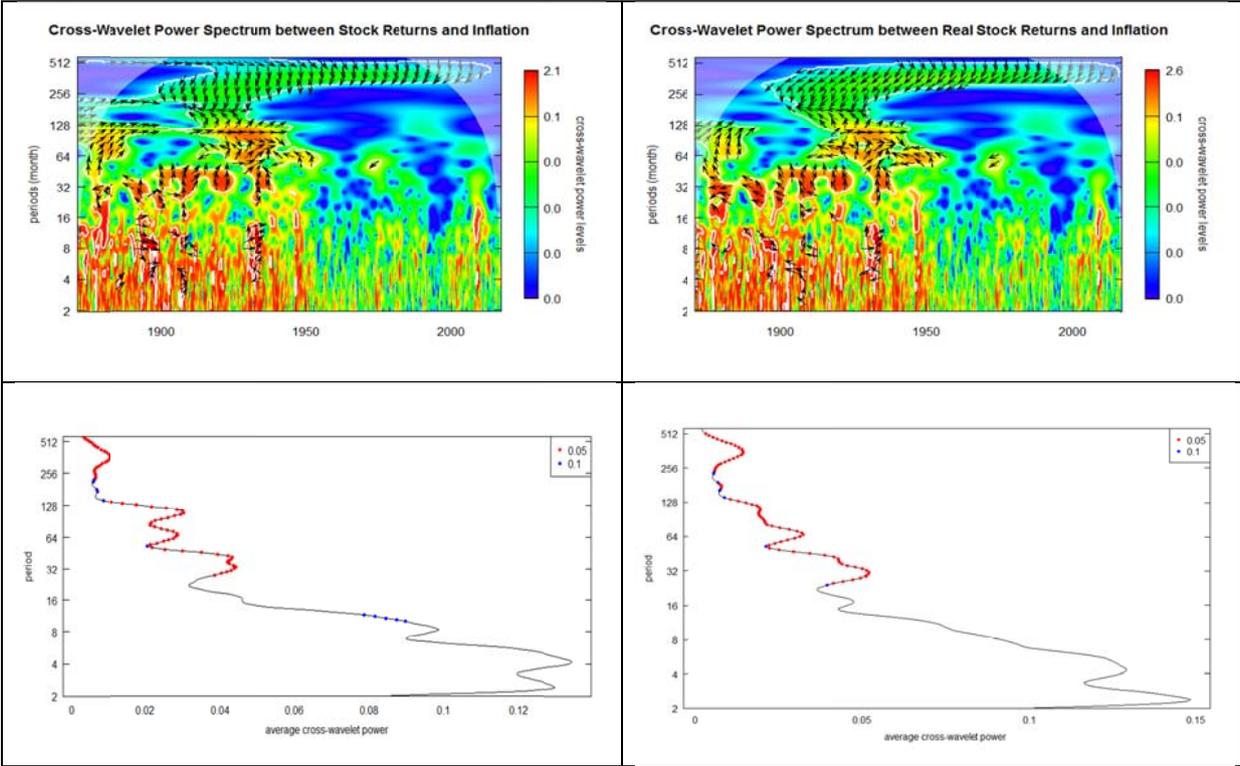
In this sub-section, we discuss in brief the results obtained for the US – a developed economy, and that for two emerging markets of South Africa and India. In the process, we compare our results with that of UK presented above. As can be seen from Figures 4 to 12, the relationship between inflation and nominal or real stock returns, especially at medium to long-run cannot be denied, as was also observed for the UK. Moreover, as with UK, the relationship is not only time-varying, but also contingent on the frequencies we are looking at. Most importantly, considering the average phase differences, we observe that in US and India, stock returns (nominal or real) are mostly anti-phase (i.e., negatively related) with

inflation, with inflation leading stock returns, as in the UK. Whenever, in-phase movements are observed as in the early part of the sample for the US, and majority of the time-period for South Africa (barring 1970s and mid-1980s when the variables are anti-phase with inflation leading stock returns, and the period of 2000-2010 when the in the negative relationship between stock returns and inflation, the former is the lead variable), stock returns lead inflation, i.e., the wealth effect is at play. So, overall our results tend to suggest that, while the relationship between stock returns and inflation varies across frequencies and time periods, there is no evidence of stock returns acting as an inflation hedge, irrespective of whether we look at developed or developing markets based on long-samples of historical data. In other words, based on our study, we can conclude that stock returns are a bad hedge against inflation.

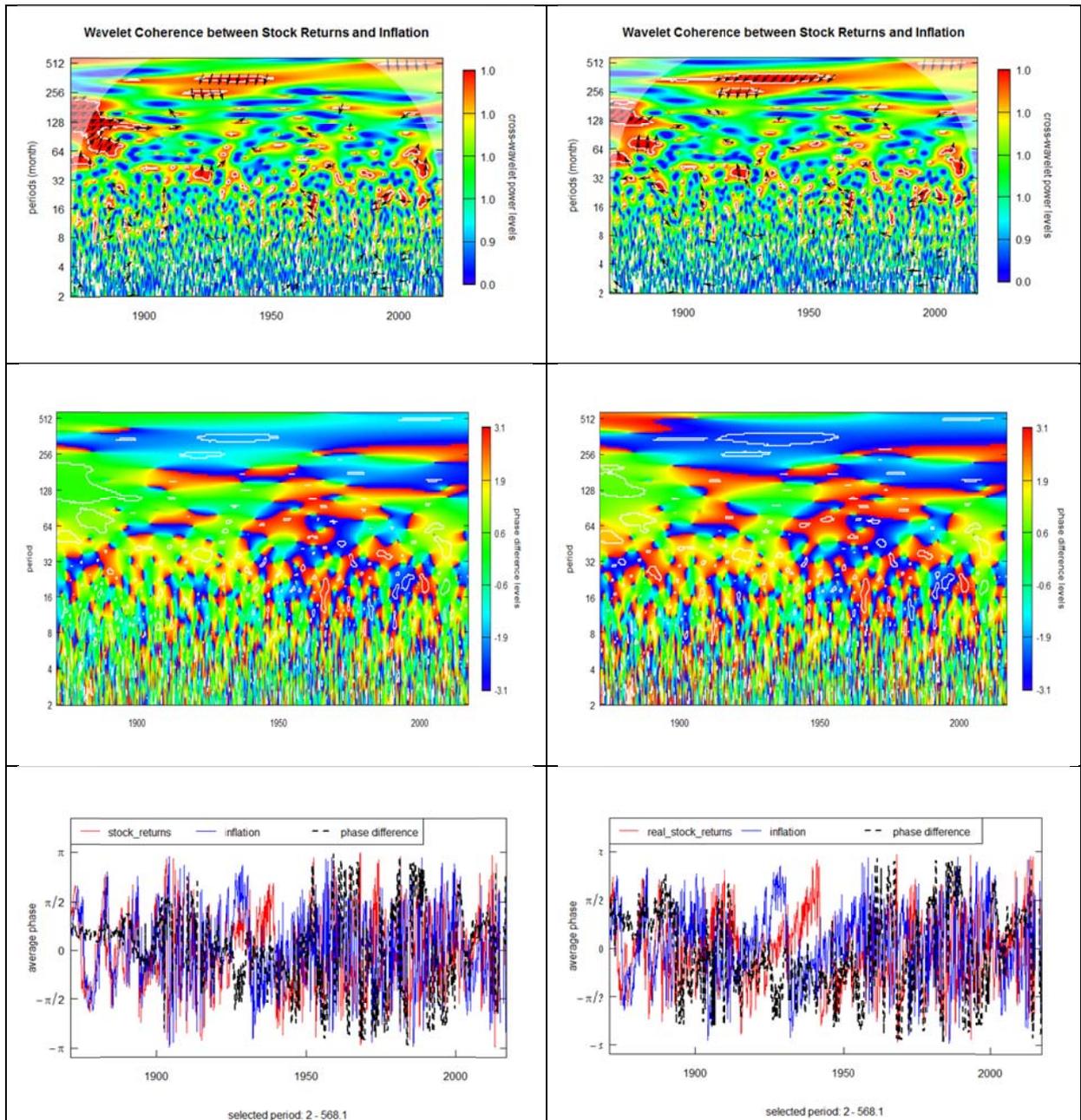
**Figure 4: WPS and average wavelet power for US**



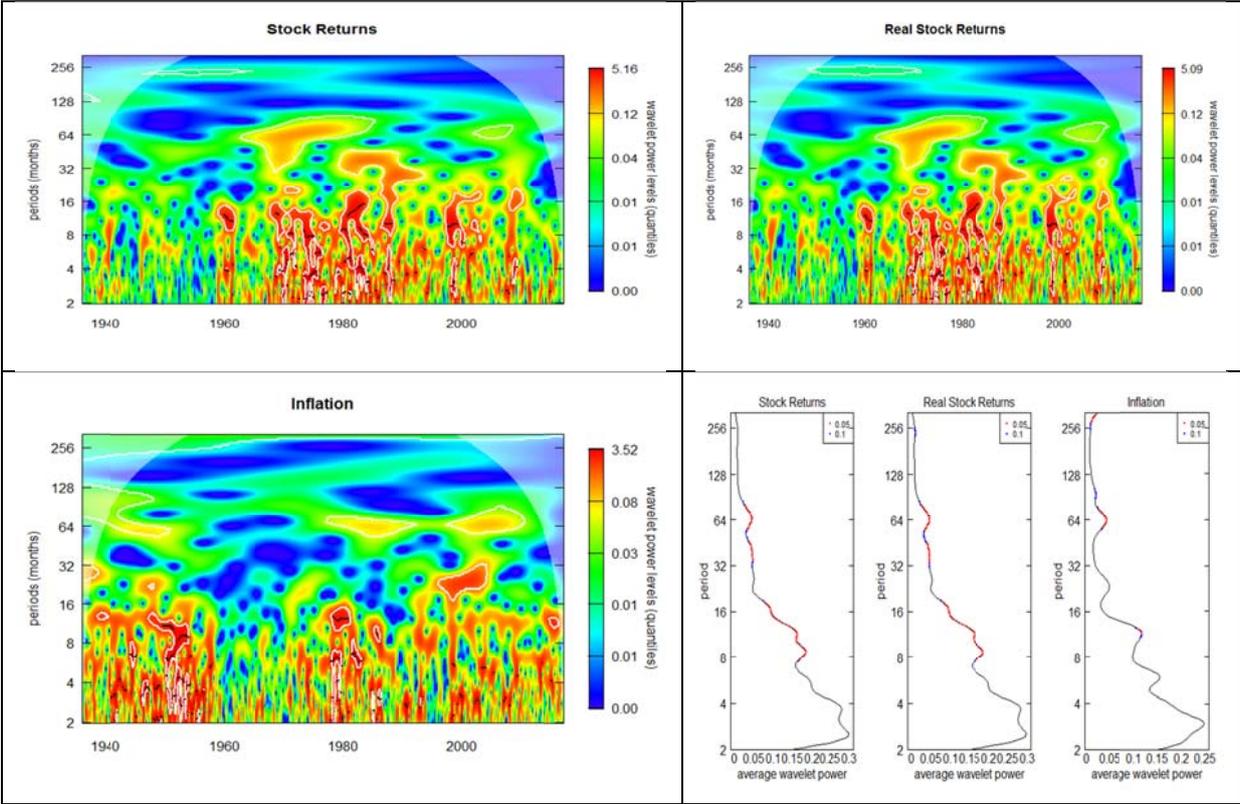
**Figure 5: Cross-Wavelet Transform (XWT) and average wavelet power for US**



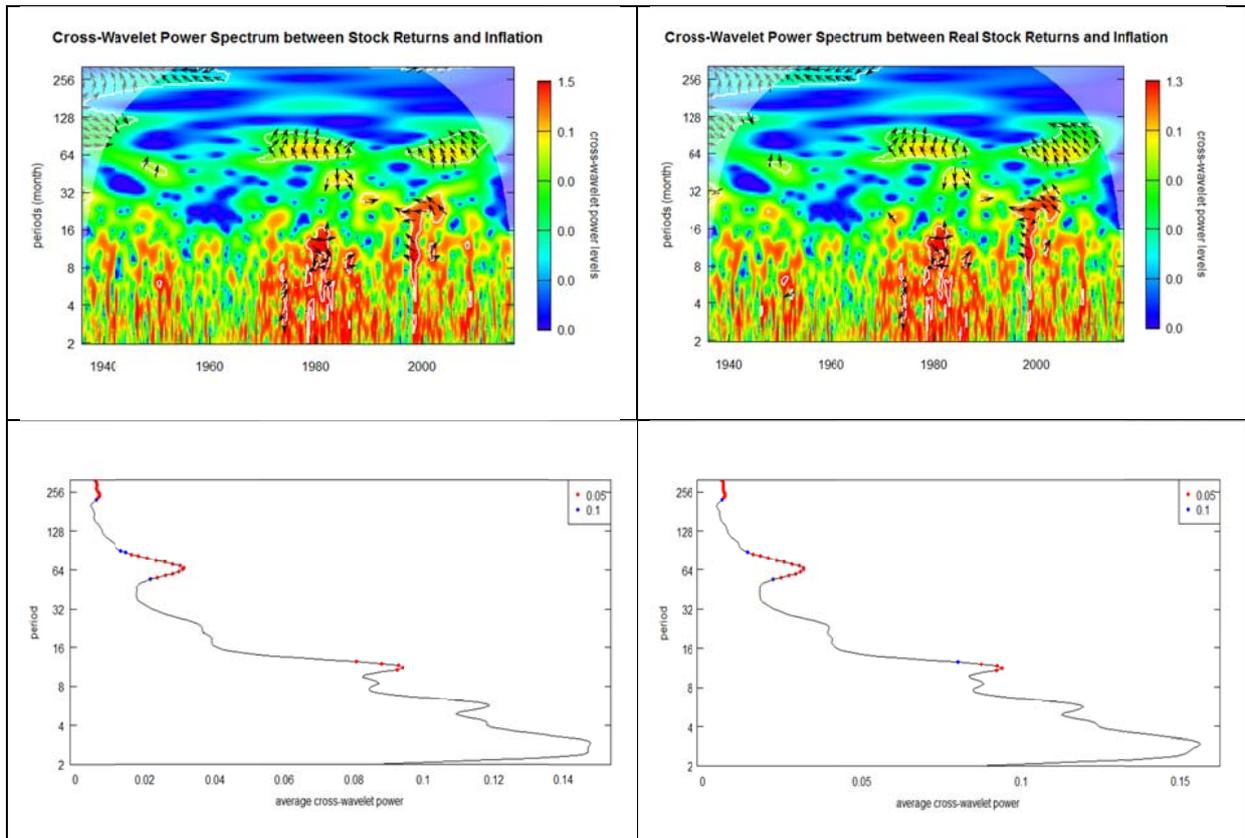
**Figure 6: Continuous Wavelet Coherence (CWT) and phase-differences for US**



**Figure 7: WPS and average wavelet power for South Africa**

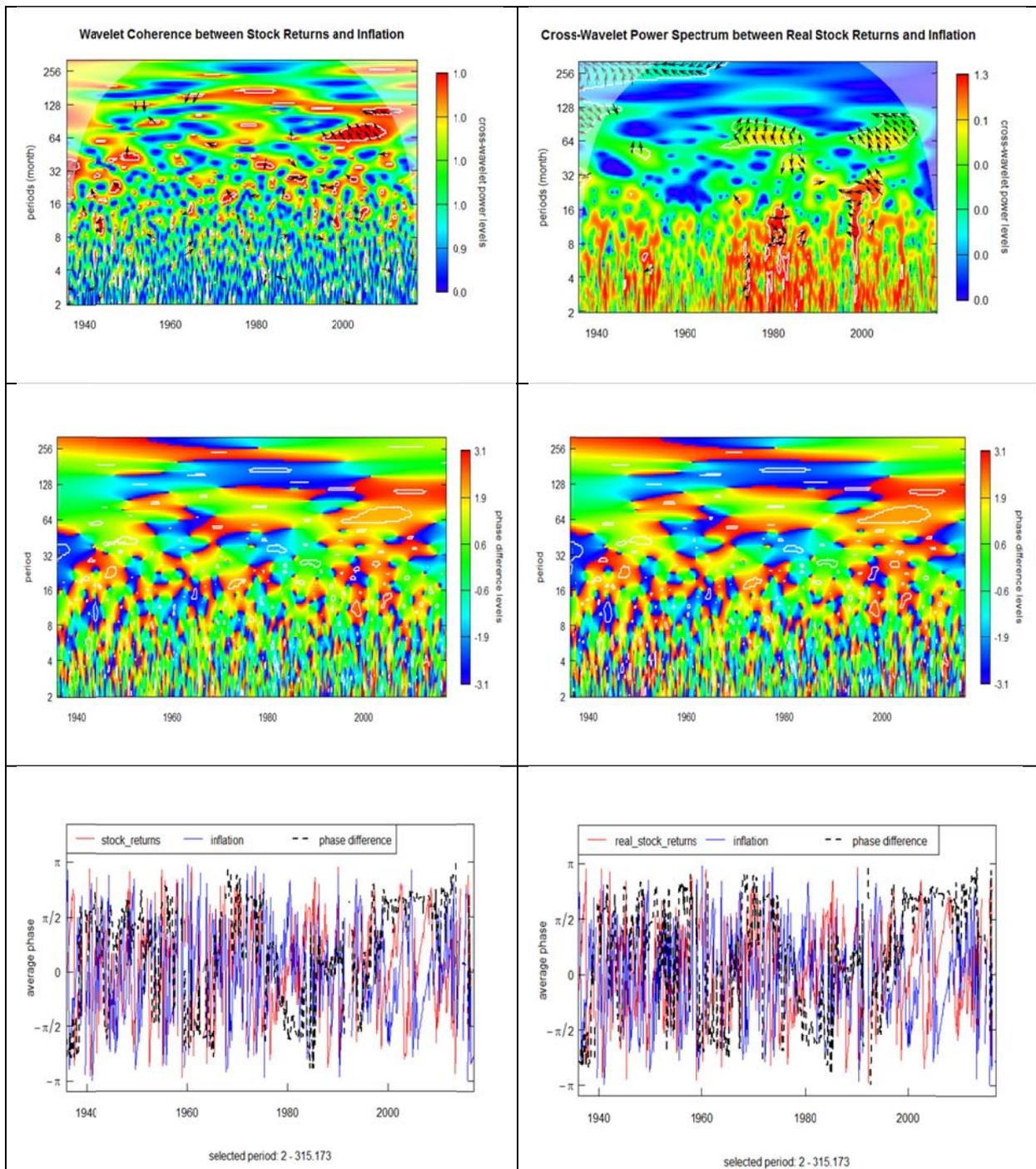


**Figure 8: Cross-Wavelet Transform (XWT) and average wavelet power for South Africa**



**Figure 9: Continuous Wavelet Coherency (CWT) and phase-differences for South**

**Africa**



**Figure 10: WPS and average wavelet power for India**

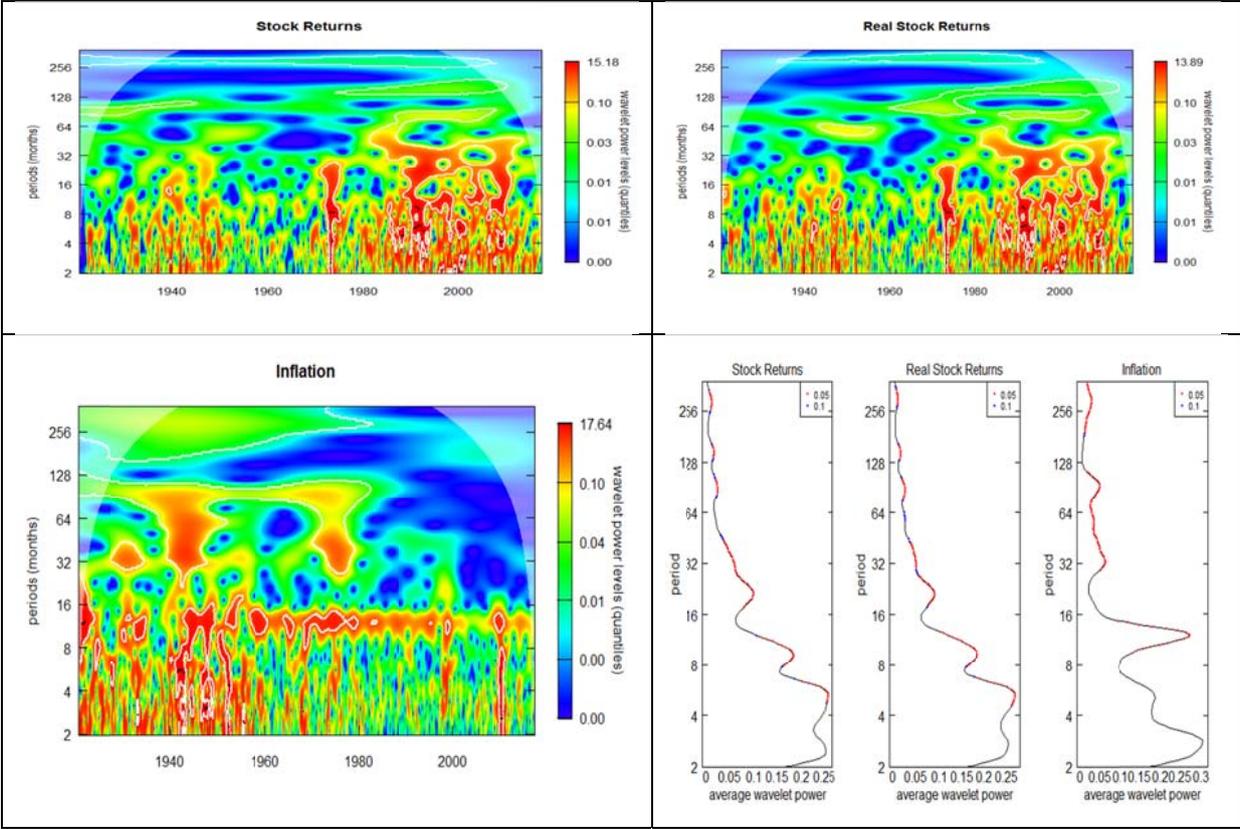
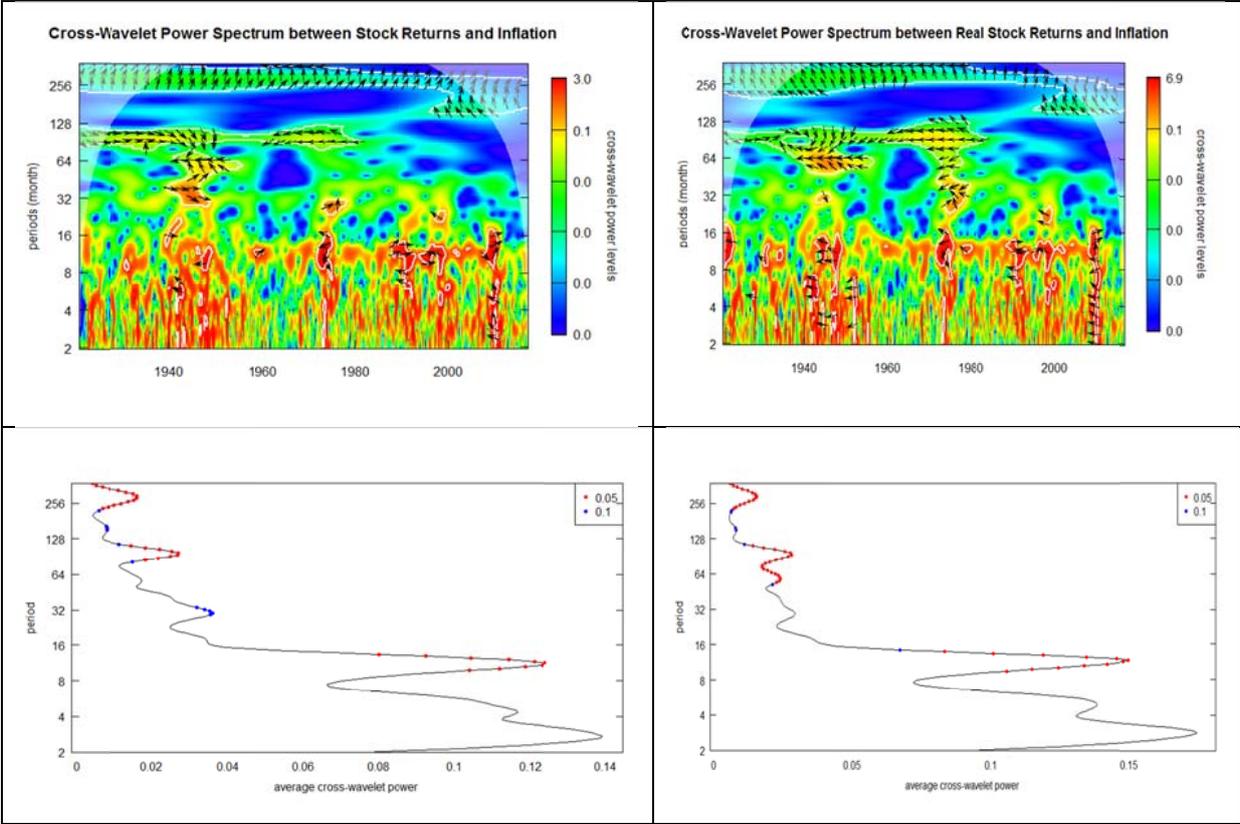
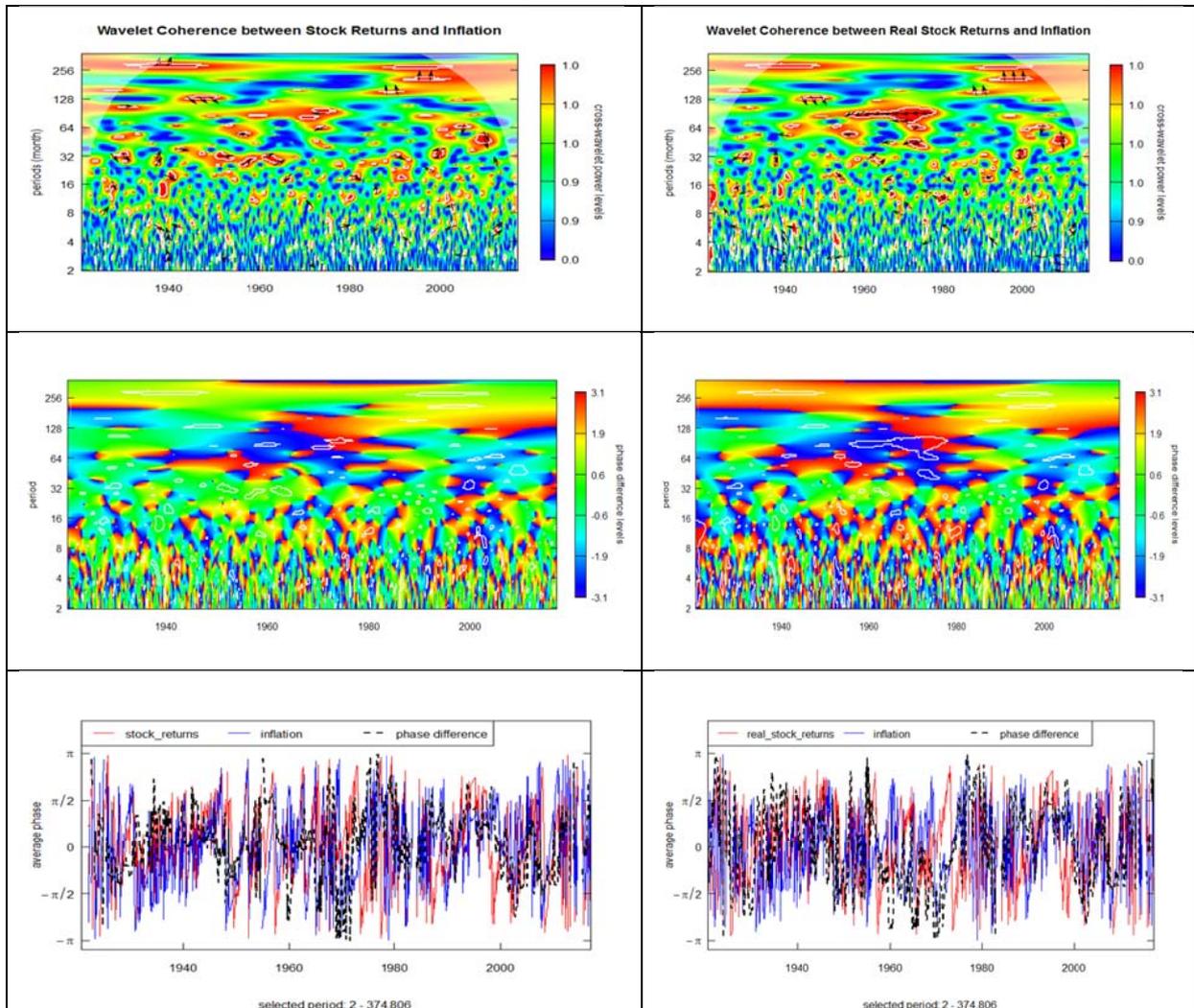


Figure 11: Cross-Wavelet Transform (XWT) and average wavelet power for India



**Figure 12: Continuous Wavelet Coherency (CWT) and phase-differences for India**



#### 4. Conclusions

The objective of this paper is to test whether stock prices can be considered an inflation hedge for the UK economy, using a long span of data which covers observations for over the last three centuries (February 1790-February 2017), by means of applying different wavelets transforms (i.e. discrete, continuous, multiple). Using this methodology, we test for the generalized Fisher hypothesis allowing for different correlation levels between inflation rates

and stock market returns at different frequency scales and at different moments in time. Furthermore, we compare the results obtained for the UK with those for the US and two developing countries (India, South Africa).

The main results of the paper can be summarized as follows. First, as assumed, our main results suggest that the relationship between inflation rates and nominal stock returns changes at different frequencies and different time periods. In particular, both variables present common movements especially in the medium- and long-run. Second, in the long-run (at more than 128 months scale), and specially over the periods prior to 1800, 1875-1890 and 1950-2000, inflation and stock returns appear negatively related, with inflation rates leading stock returns. Based on the theories mentioned in the introduction, we could conclude that for these time periods, the Fisher and the Wealth Effect Hypothesis could be rejected in favor of the Money Illusion, Tax Effect, Proxy Effect and/or Reverse Causality Hypotheses. In contrast, and for the time periods 1800-1870, 1900-1950 and post 2000, characterized in general for lower inflation rates, the results suggest the existence of a positive relationship between the variables with stock returns leading inflation rates. That is, for these periods, the results support the Wealth Effect Hypothesis, but not the Fisher Hypothesis, so that we can conclude that stock returns are not a hedge against inflation. Finally, when we compare the results for the UK case with those for the US, India and South Africa, they again suggest that there is no evidence of stock prices acting as an inflation hedge, irrespective of whether we look at developed or developing economies.

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## Appendix:

Figure A1. Nominal Stock Returns, Inflation Rates and Real Stock Returns

