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## February 2015



# Analysis and Optimisation of a Receiver Tube for Direct Steam Generation in a Solar Parabolic Trough Collector

Henriette Nolte<sup>1</sup>, T. Bello-Ochende<sup>2</sup> and J.P. Meyer<sup>1</sup>

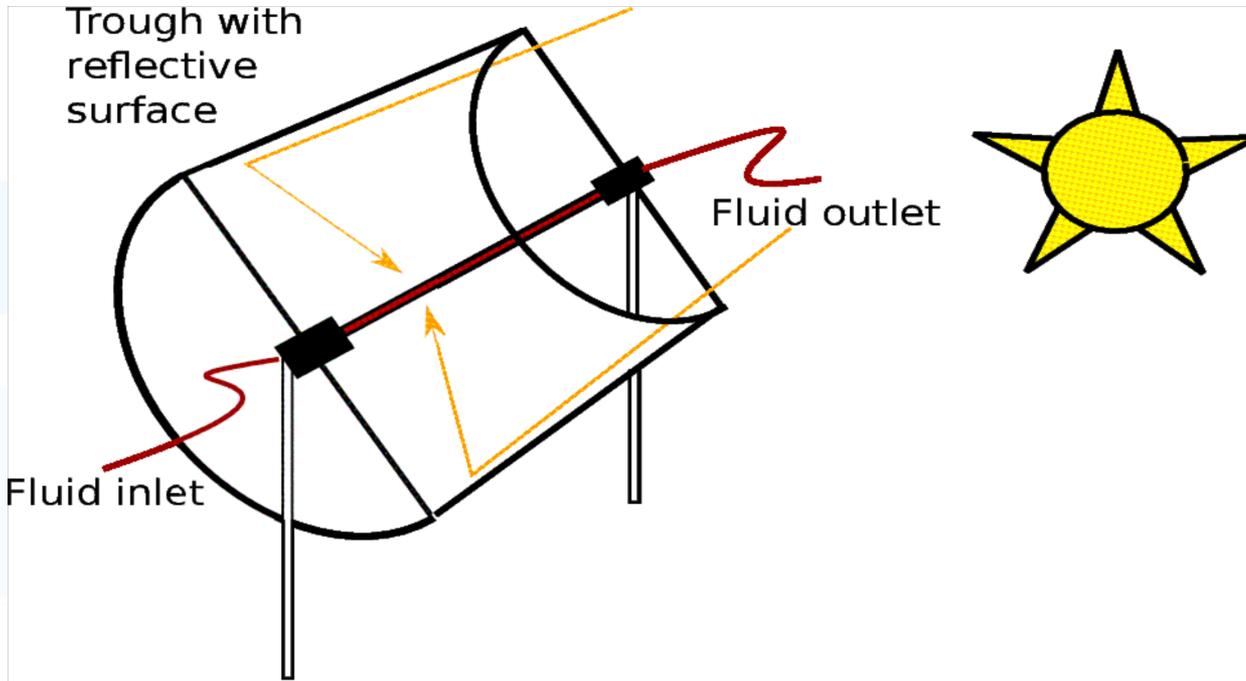
<sup>1</sup>Department of Mechanical and Aeronautical Engineering  
University of Pretoria, Pretoria, South Africa, 0002

<sup>2</sup>Department of Mechanical Engineering  
University of Cape Town, Rondebosch, South Africa, 7701

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# Parabolic Trough



## Advantages

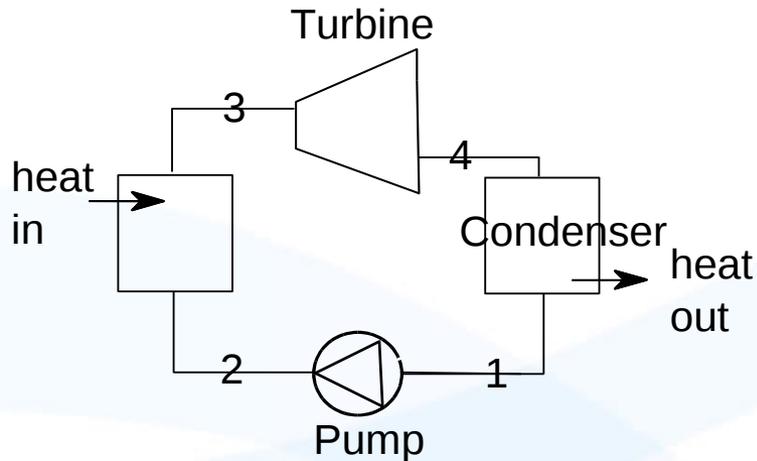
- One Axis Tracking
- Moderate Temperatures (200 – 400 °C)
- Water can be used as working fluid
- Tried and tested technology

## Disadvantages

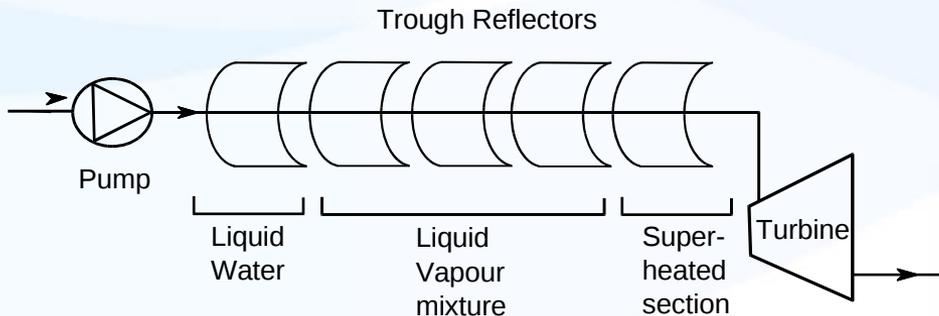
- Water not as thermally stable as thermal oil
- Lower temperatures means smaller temperature differential (Disadvantage/Advantage)



# Background and Scope



## Simple Rankine Cycle



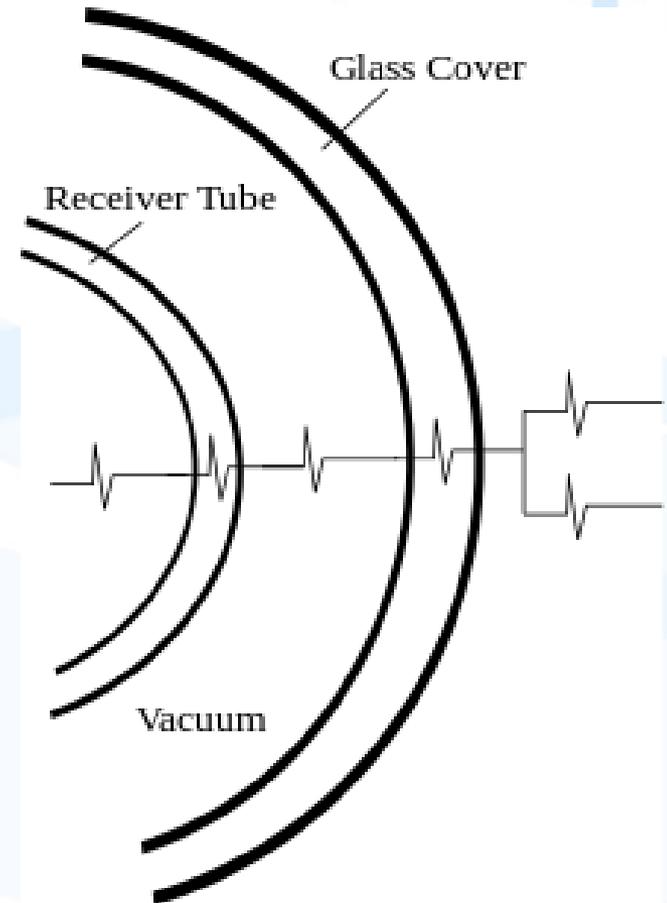
**Focus: Receiver tube**  
**Small scale:**  
**50-350kW turbine work**



# Receiver Thermal Analysis

## 1D Heat Transfer through receiver:

- Convection on inner tube perimeter
- Conduction through receiver tube wall
- Radiation from receiver tube to inner glass cover (if vacuum is maintained)
- Conduction through the glass cover
- Radiation losses from the cover
- Convection losses due to wind or natural convection
- Forced convection investigated with wind velocity of 2 m/s



# Heat Transfer and pressure drop correlations

## Single phase regions:

Use of Gnielinsky for inner tube heat transfer coefficient  
Friction factor: Petukhov for smooth tubes

## Two-phase region:

Method described by Wojtan et al.<sup>1</sup> for heat transfer coefficient

Two-phase pressure drop obtained by Friedel correlation

## Forced convection on outer glass cover:

Churchill and Bernstein

# First law analysis

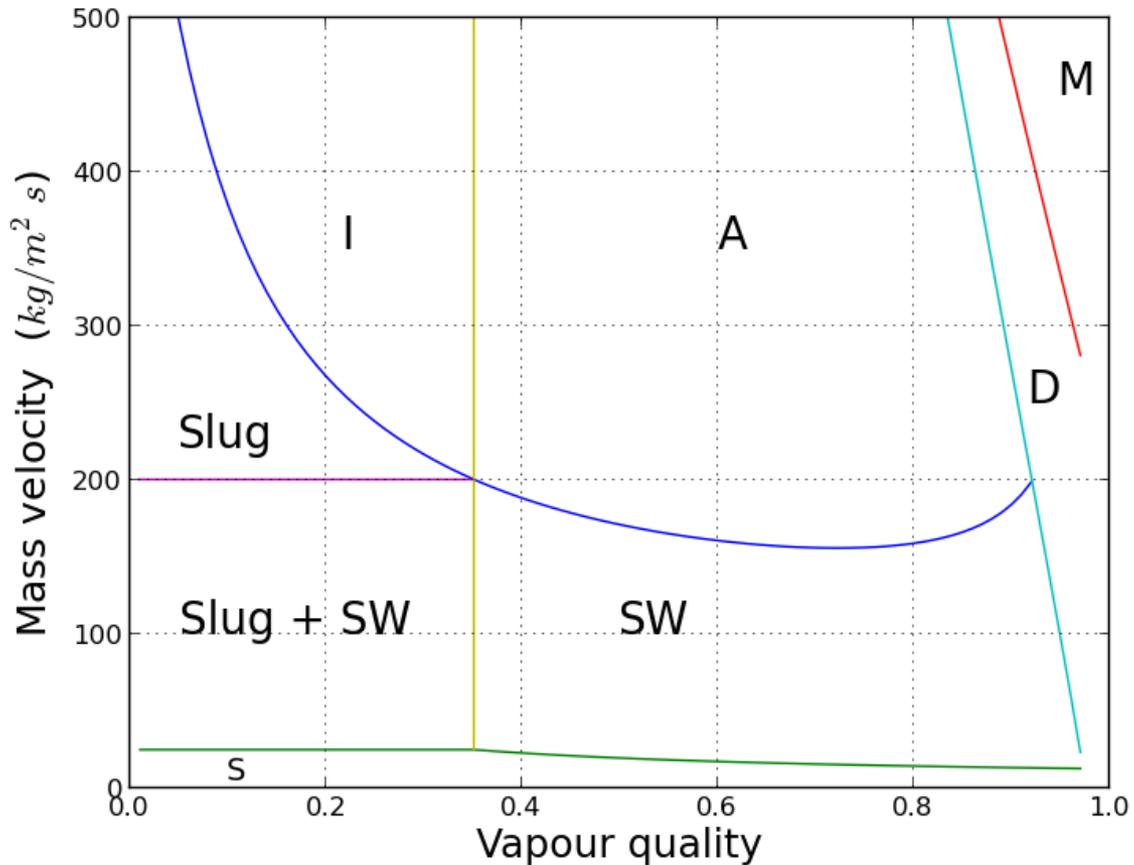
## Single phase regions

- Single phase regions (liquid and superheated region) , fluid temperature increase
- Regions divided into unit sections
- Each unit section solved iteratively in Python
- Glass cover temperature determined by energy balance and SciPy fmin

$$Q_{\text{rad, rec-cover}} = Q_{\text{conv, cover-amb}} + Q_{\text{rad, cover-sky}}$$

- Fluid properties temperature dependent
- Fluid properties obtained with CoolProp<sup>2</sup>

# First law analysis: Two-phase region



- Sections solved for each 2% quality change
- Flow regime determines heat transfer coefficient
- Heat transfer coefficient large for two-phase flow
- Receiver temperature stays reasonably constant for most part of the region
- Temperature spikes perceived when dryout occurs



# Pressure Drop

## Single phase regions (Darcy Weisbach):

$$\Delta P_{fric} = f \left( \frac{L}{D_i} \right) \left( \frac{\rho}{2} \right) V^2$$

## Two phase regions (Friedel):

$$\Delta P_L = 4f_L \left( \frac{L}{D_i} \right) \left( \frac{1}{2\rho_L} \right) G^2$$

$$\Delta P_{two-phase} = \Delta P_L \Phi^2$$

## Limitation:

Momentum and Static losses not taken into account  
To avoid added uncertainty of layout and fittings



# Second Law Analysis

## Entropy Generation due to<sup>3</sup>:

### 1) Finite temperature differences

$$S_{gen,dT} = \frac{E_{des}}{T_{amb}}$$

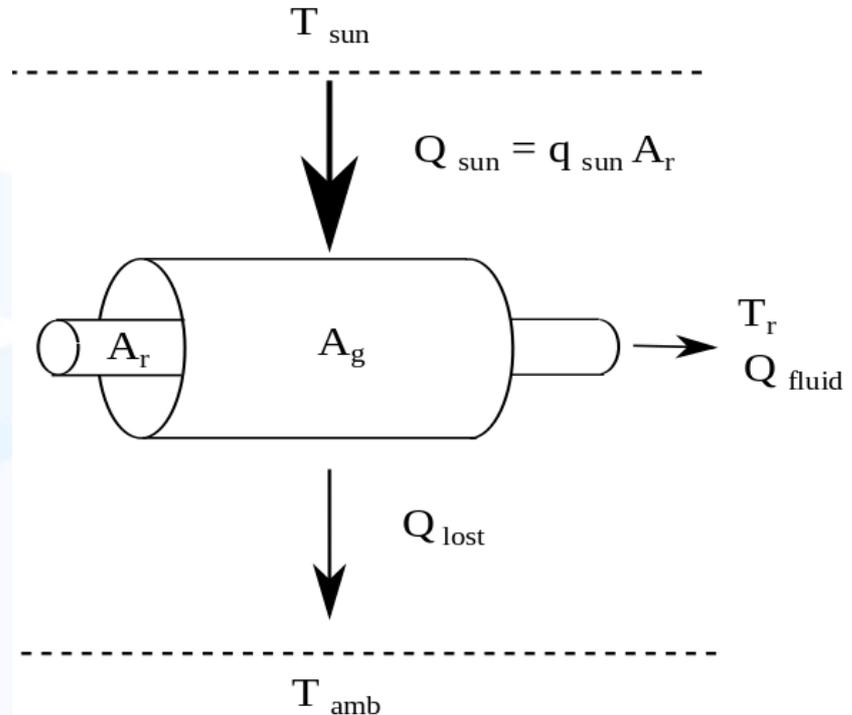
#### Exergy Destruction

$$E_{in} = Q_{sun} (1 - T_{amb}/T_{sun})$$

$$E_{out} = Q_{fluid} (1 - T_{amb}/T_r)$$

$$E_{des} = E_{in} - E_{out}$$

$$S_{gen} = E_{des}/T_{amb}$$



# Second Law Analysis

## 2) Entropy Generation due to fluid friction:

$$S_{gen,dP} = \frac{\dot{m} \Delta P}{\rho T}$$

### Initial Parameters

$T_{amb}$	20°C
$Q_{sun}$	2000 W
Turbine inlet	20% higher than $T_{cat}$
$T_{sky}$	12°C



# Validation: Single Phase Region

## Heat losses throughout the liquid region and superheated region

- Base case parameters:

$T_{\text{sat}} = 250 \text{ }^\circ\text{C}$  (4 MPa),  $m = 0.2 \text{ kg/s}$ ,  $D_i = 25 \text{ mm}$

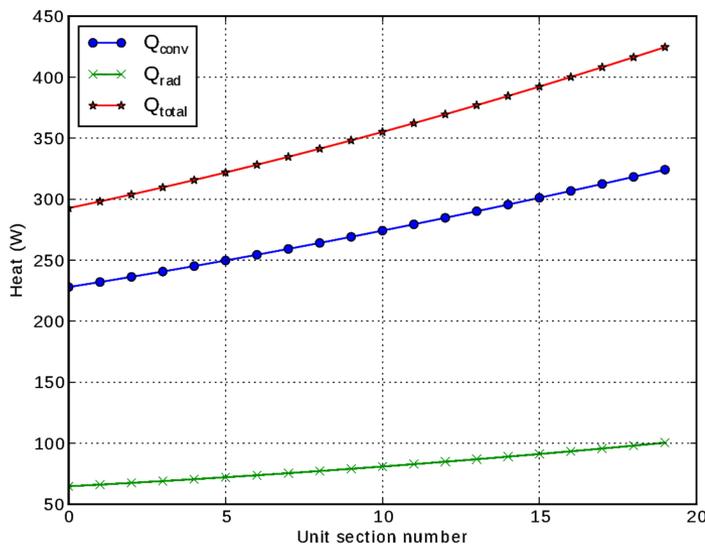
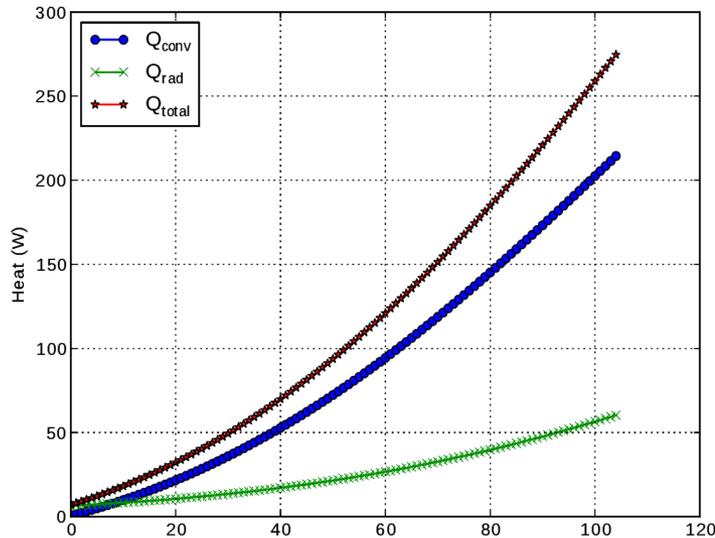
- Initially radiation losses higher than convection

- Convection losses small initially

- Glass cover initially close to ambient for first 5 - 10 unit sections

- Liquid region much longer than superheated region

- Losses highly depended on cover temperature

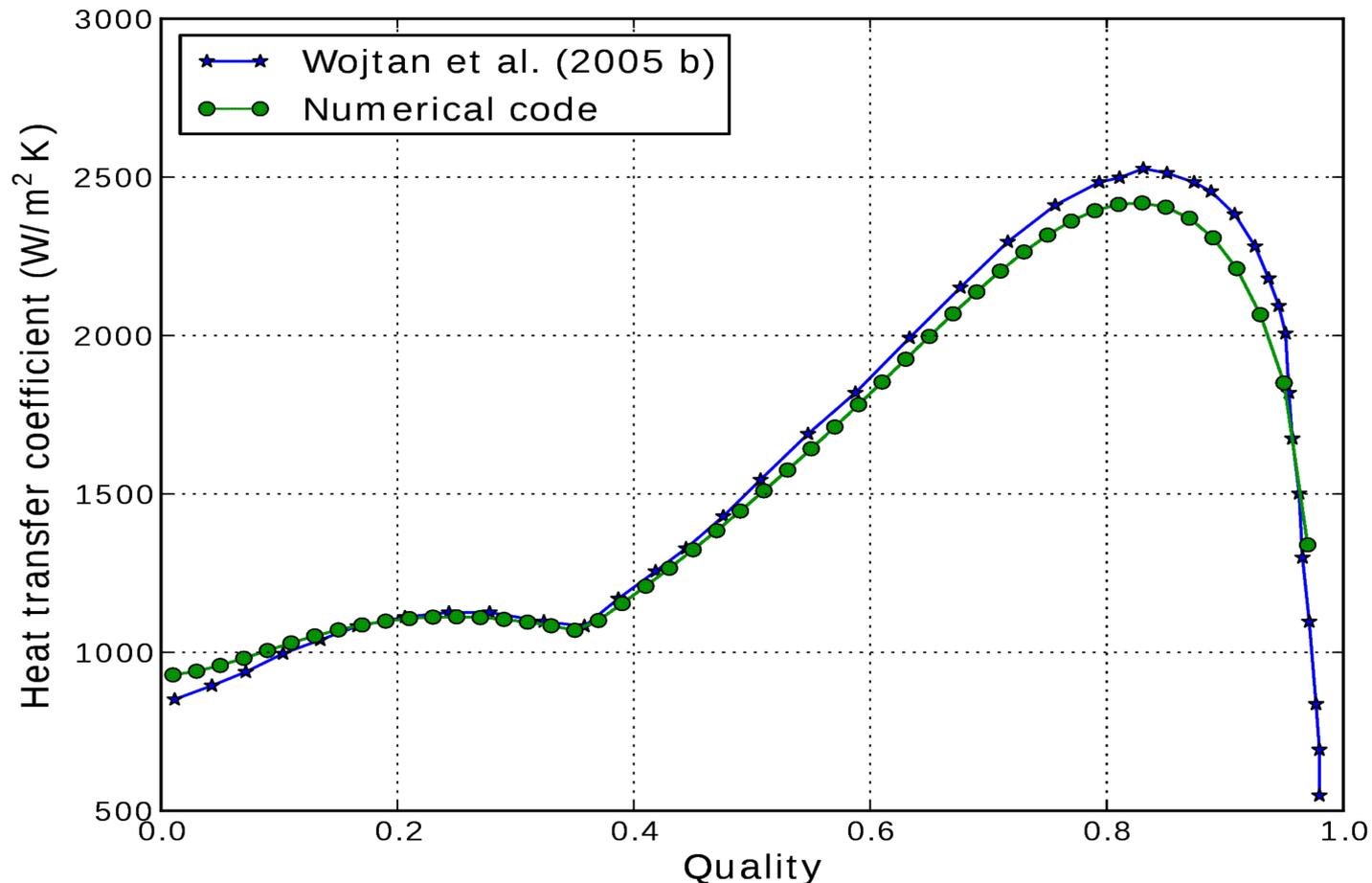


# Validation: Two-phase region

Heat transfer coefficient comparison for R22 with following parameters:

$T_{\text{sat}} = 5 \text{ }^\circ\text{C}$  ,  $G = 150 \text{ kg/m}^2\text{s}$  (mass velocity),

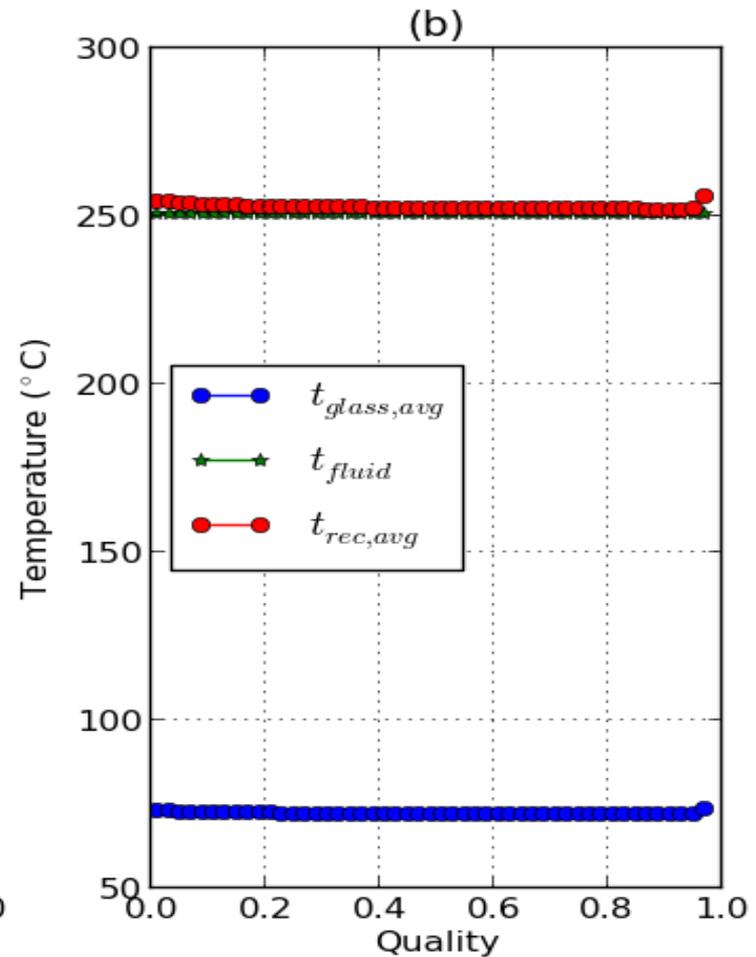
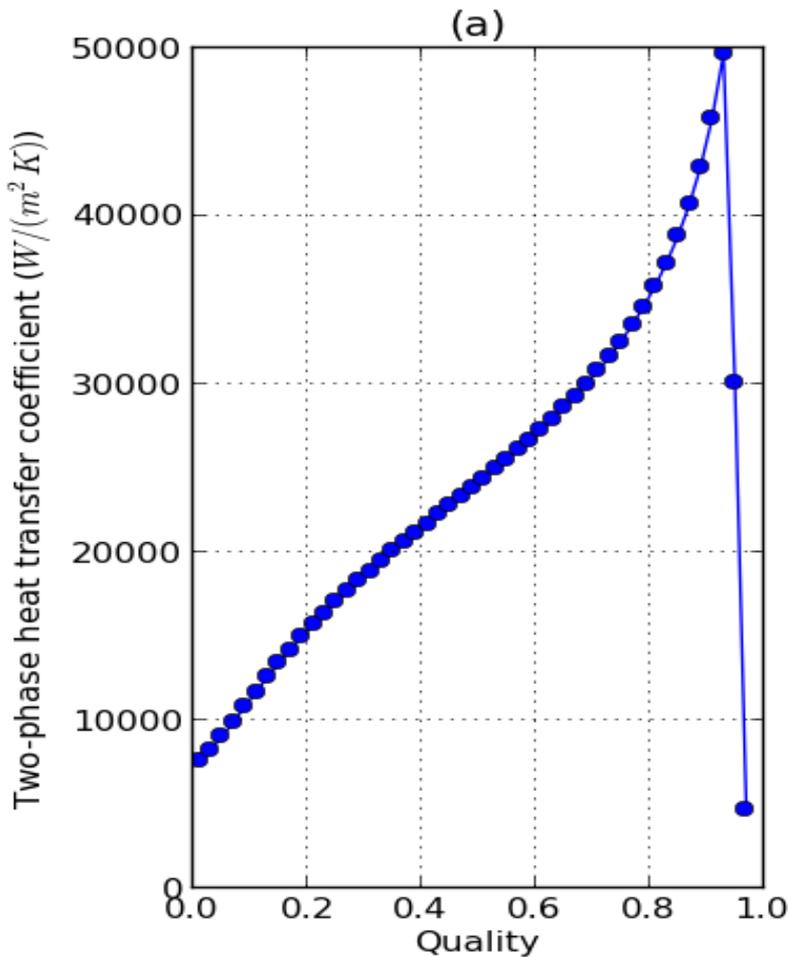
$D_i = 13.84 \text{ mm}$  ,  $q = 3.6 \text{ kW/m}^2$



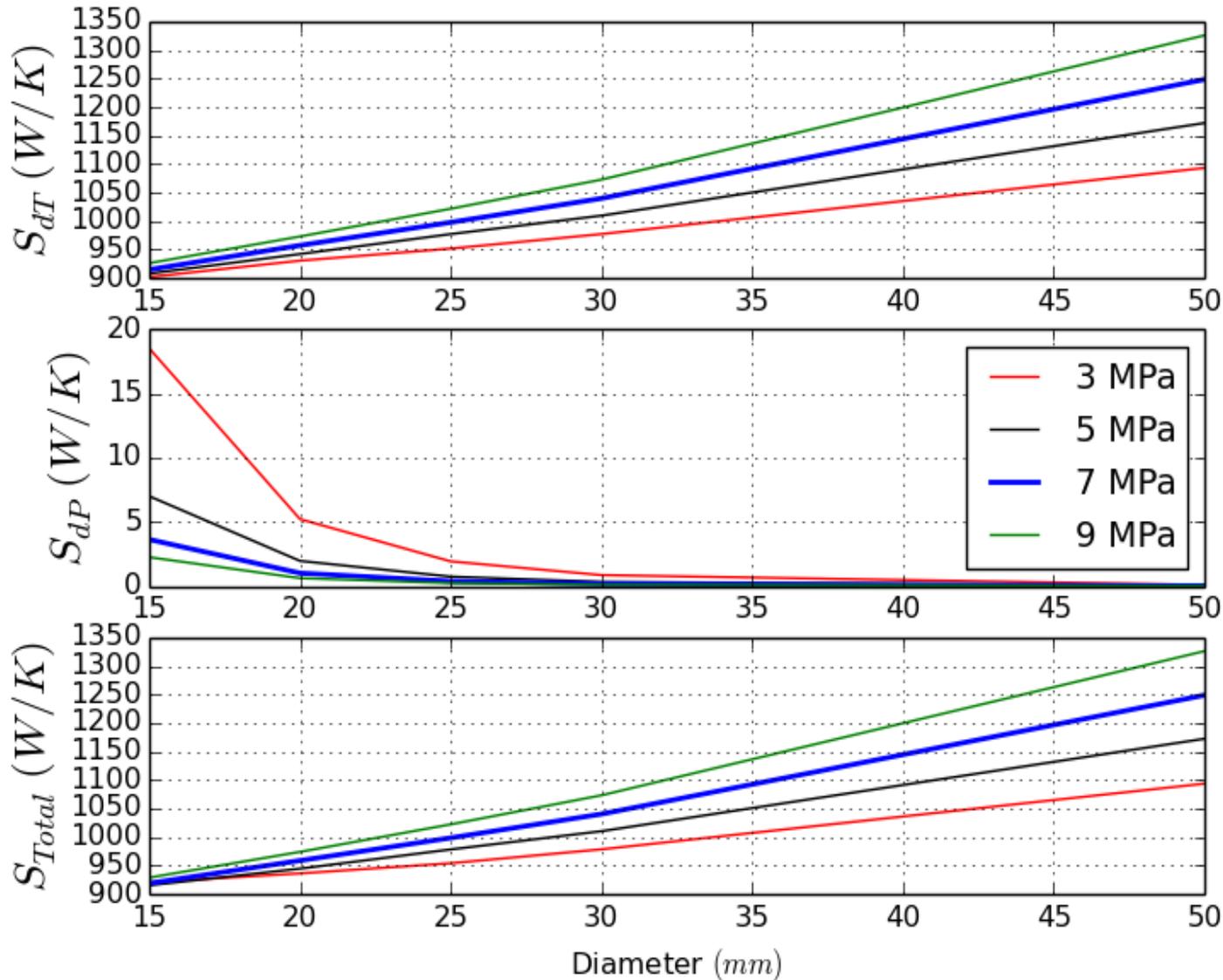
# Validation: Two-phase region

Heat transfer coefficient comparison for base case parameters:

$$T_{\text{sat}} = 250 \text{ }^\circ\text{C} , m = 0.2 \text{ kg/s} , D_i = 25 \text{ mm} , Q = 2 \text{ kW/m}$$



# Results: Low mass flow



-  $S_{gen,dT}$  = Finite Temperature differences

-  $S_{gen,dP}$  = Fluid friction

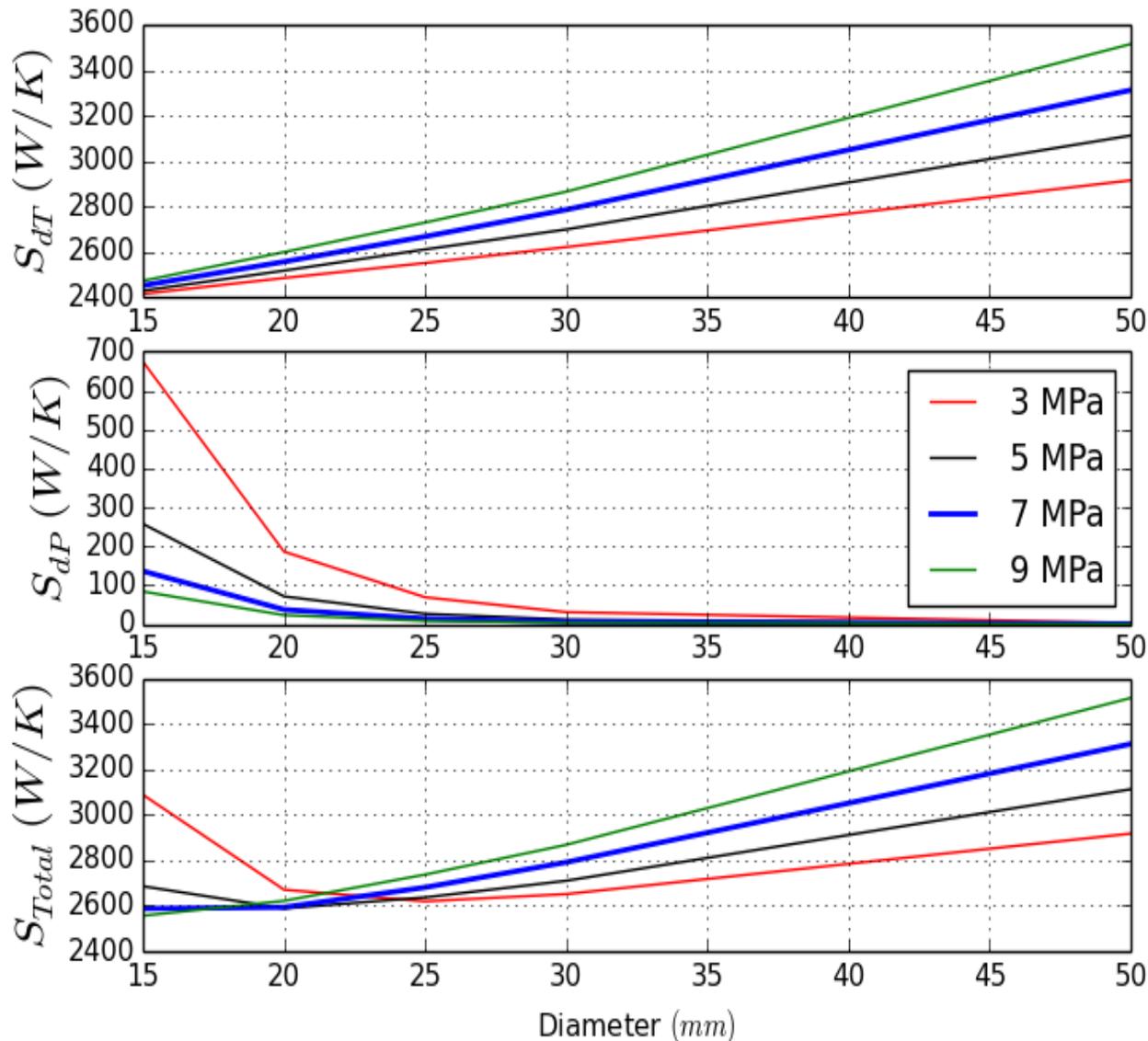
-  $S_{gen,dT}$  increases with increase in diameter

-  $S_{gen,dP}$  decreases with increase in diameter

-  $S_{gen,dP}$  small to negligible influence on the total entropy generation

-  $S_{gen,dP}$  only influences smallest diameter at smallest operating pressure

# Results: High mass flow



-  $S_{gen,dT}$  = Finite Temperature differences

-  $S_{gen,dP}$  = Fluid friction

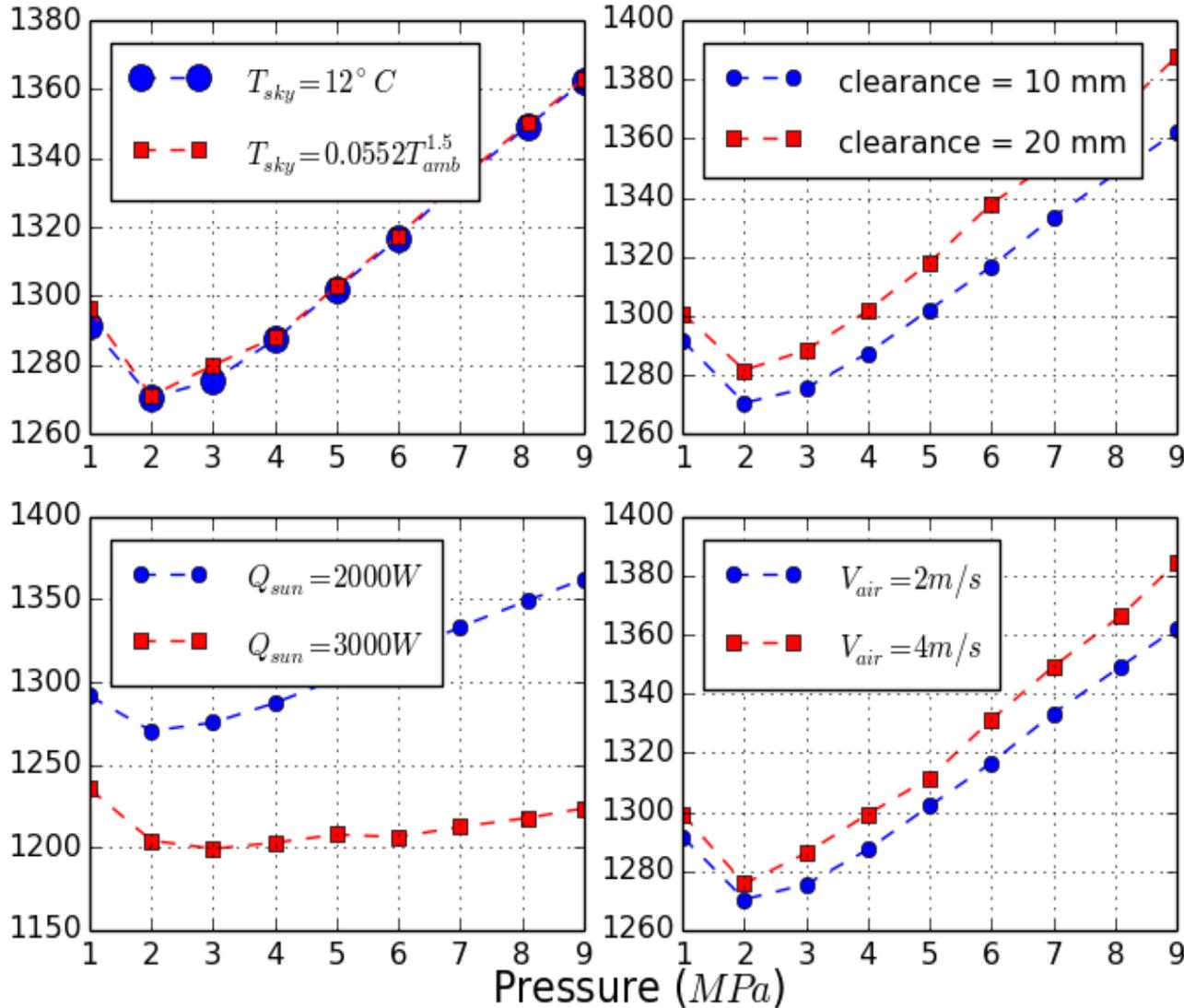
-  $S_{gen,dP}$  larger influence for the high mass flow rate case

- Higher  $S_{gen,dP}$  values not only due to more fluid but due to fluid friction becoming significant for small diameters

- Effect noticeable for operating pressures 3 and 5 MPa

# Sensitivity Analysis

Total Entropy Generation (W/K)

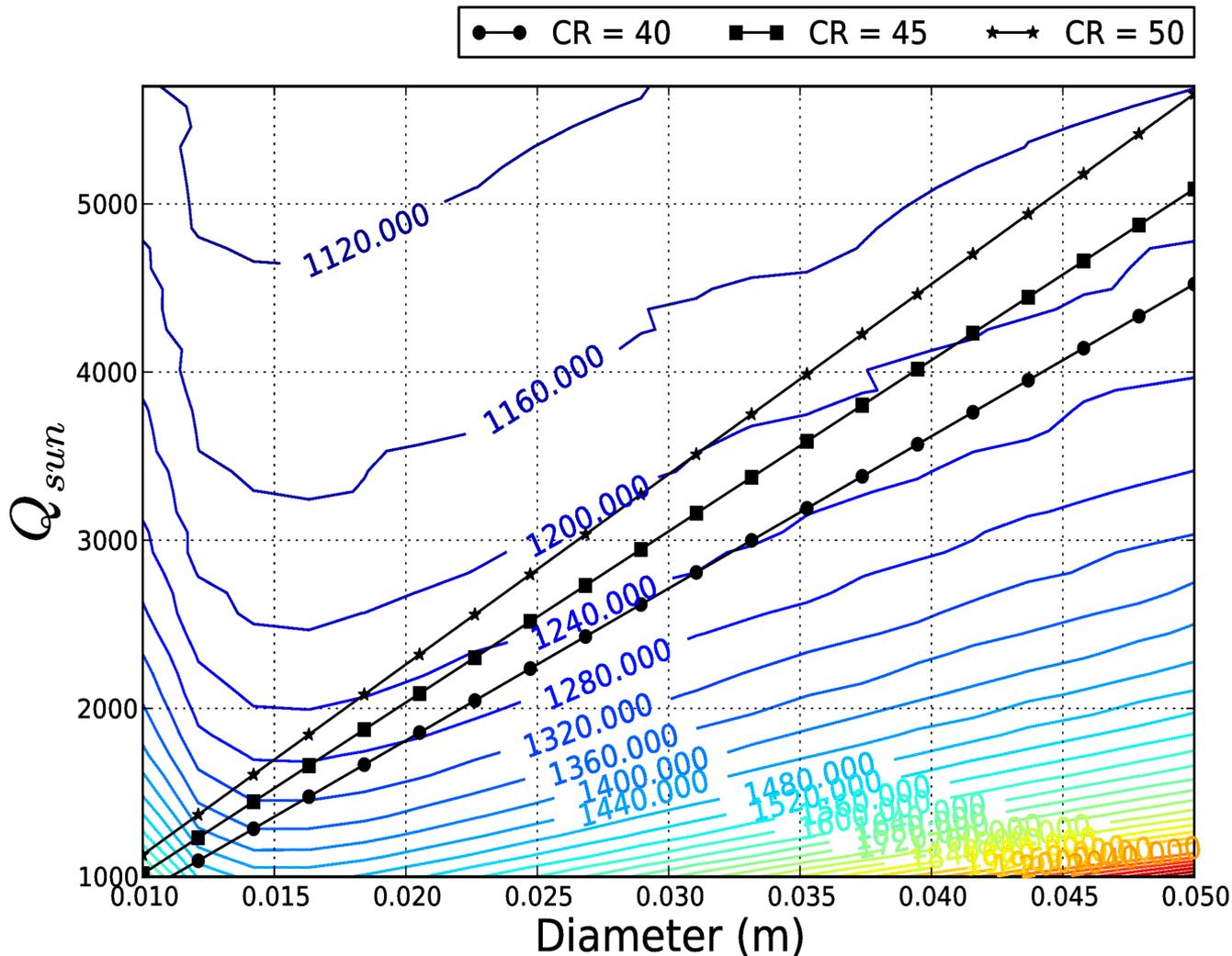


- Effective sky temperature minimal effect on  $S_{gen}$

- Clearance and wind velocity only influences value of  $S_{gen}$  but not the minimum

-  $Q_{sun}$  shifts minimum

# Optimisation



- CR (concentration ratio) constraint line

-  $10 \text{ mm} < D_i < 15 \text{ mm}$  influences of fluid friction can be seen

-  $D_i > 15 \text{ mm}$  mostly influenced by  $S_{gen, dT}$

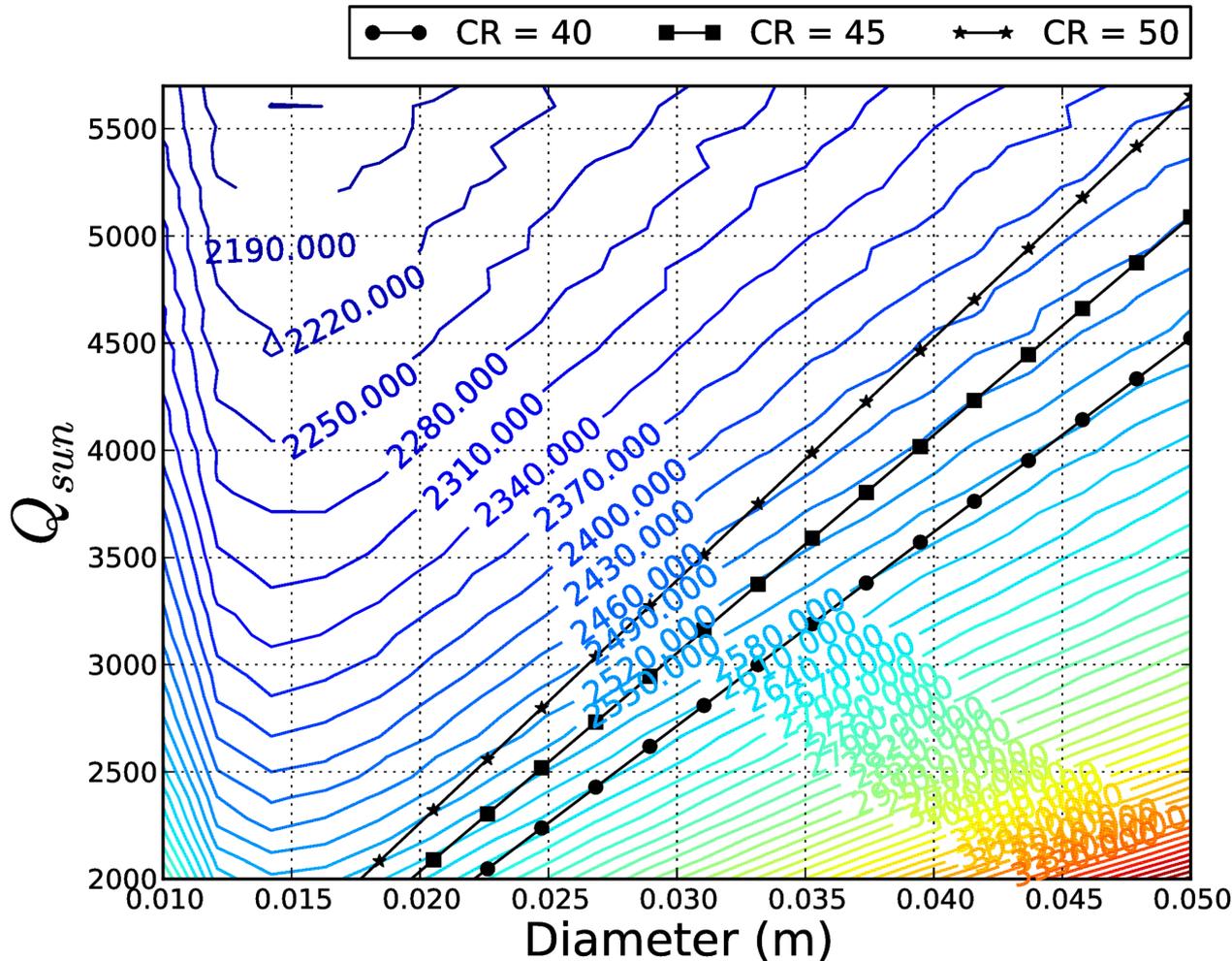
- Higher CR means closer to optimality

- Constraint lines steeper than contour lines, if  $Q_{sun}$  and  $D_i$

increased  $S_{gen}$  can be lowered but effect diminishes for larger  $D_i$

Case:  $T_{sat} = 250 \text{ }^\circ\text{C}$  (4 MPa),  $m = 0.2 \text{ kg/s}$

# Optimisation



- CR (concentration ratio) constraint line

- Contour lines representing  $S_{gen,dT}$  component slightly steeper for case  $T_{sat} = 310\text{ }^{\circ}\text{C}$  vs  $T_{sat} = 250\text{ }^{\circ}\text{C}$

- Higher temperatures and temperature differential will mean more entropy generation due to finite temperature differences  $S_{gen,dT}$

# Optimisation

## Simulated Annealing (SA) Optimisation

- Function not entirely smooth
- SA doesn't use gradient information
- Available in Python (SciPy)
- Based on process of annealing molten metal

Table 1: Global Optimum

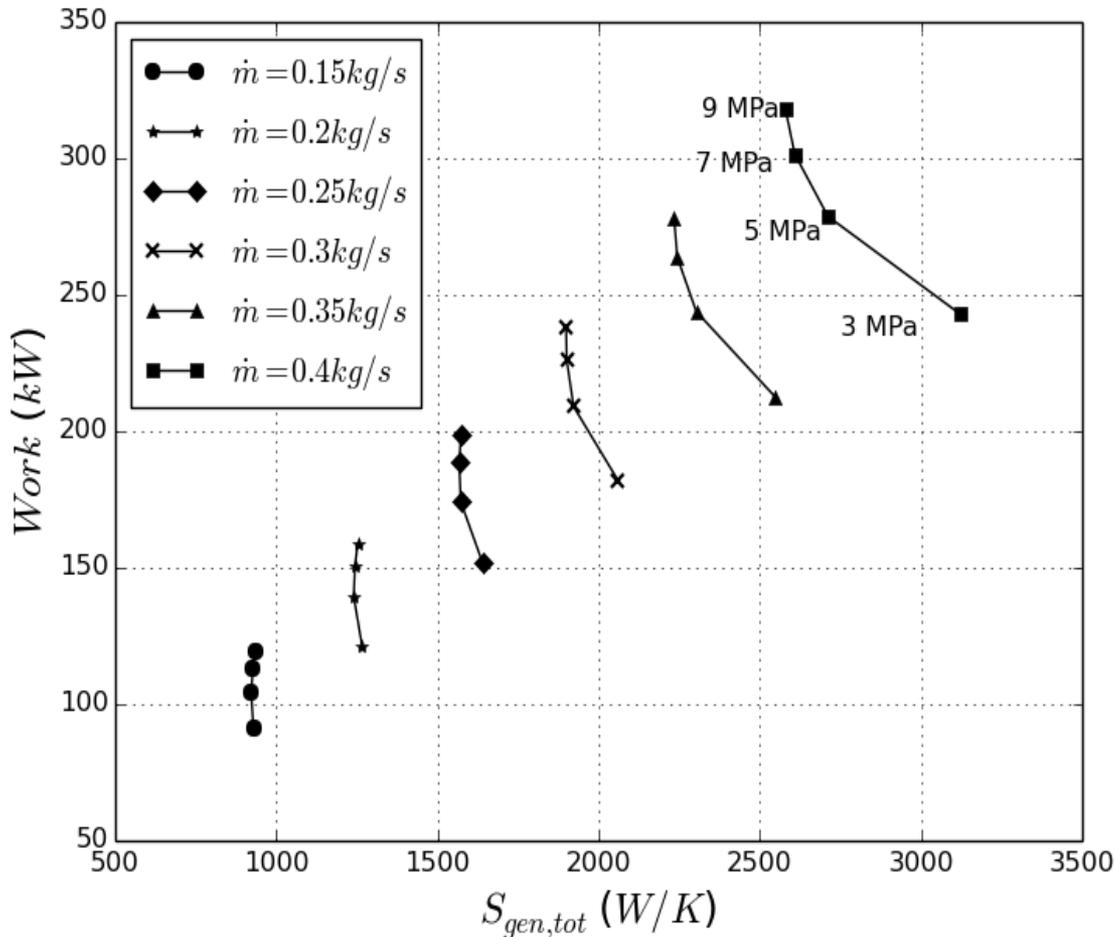
Parameter	Optimal
$D_i$	44.6 mm
Mass flow	0.1513 kg/s
Pressure	7.62 MPa
Total Entropy	899.14 W/K

Table 2: Optimal Pressure for various flow rates,  $D_i = 20$  mm

Mass flow (kg/s)	Optimal Pressure (MPa)	Total Entropy (W/K)
0.15	3.597	903
0.2	3.815	1211
0.25	3.948	1523
0.3	4.68	1838
0.35	5.47	2156
0.4	6.715	2478



# Multi-Objective Optimisation



- Higher mass flow; more work output

- Higher mass flow rate is influenced by  $S_{gen,dP}$  at lower operating pressures (3 and 5 MPa)

- Lower mass flow rates (0.15 kg/s) hardly influenced by  $S_{gen,dP}$

- Outcome will change for other cases where tube diameters are larger

# Conclusions

- Two-phase region long for low operating pressure

Higher Enthalpy of Evaporation

3 MPa:  $h_{fg} = 1796$  kJ/kg      VS      9 MPa:  $h_{fg} = 1379$  kJ/kg

- Long two-phase regions result in larger contributions from  $S_{gen, dP}$

- For most cases  $S_{gen, dT}$  contributes more significantly to the total entropy generation

(Especially at diameters larger than 20 mm and when concentration ratio constraints are taken into account)

- Larger concentration ratios result in less entropy generation

- If  $Q_{sun}$  is constant it will always be more advantageous to consider smaller diameters

- If the CR is kept constant increasing the diameter will tend to decrease  $S_{gen}$



# Conclusions

- Simulated Annealing optimisation
- Optimal Operating pressure increases if mass flow rate is increased
- Higher operating pressures slightly increase  $S_{gen}$  but are more advantageous because more available work
- Operating pressures lower than 3 MPa is not recommended due to large  $S_{gen, dP}$  contributions and excessive and small work output

## Future Work

- Heat transfer enhancement
- Cost Analysis



**Thank You**



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